

# WG2 Highlights

## Small $x$ , Diffraction and Vector Mesons Theory

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XXI International Workshop on Deep-Inelastic Scattering and Related Subjects  
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Thank you to all participants! 40 talks

Theory and phenomenology

Recent theoretical developments on high-energy effective theories

Victor Fadin, Martin Hentschinski, Grigorios Chachamis, Handreas Van Hameren

High density, saturation

Adrien Besse, Michal Deak, Krzysztof Kutak, Stéphane Munier, Cyrille Marquet, Amir Rezaeian

Exclusive processes related issues

Franck Sabatié, Ruben Sandapen

Testing QCD in the perturbative Regge limit at LHC

Cristiano Brenner Mariotto, Michal Deak, Bertrand Ducloué, Wolfgang Schaefer, Antoni Szczurek

Multiparton interactions

Markus Diehl, Emilia Lewandowska

The Regge limit at LHC

Daniel Fagundes, Antoni Szczurek

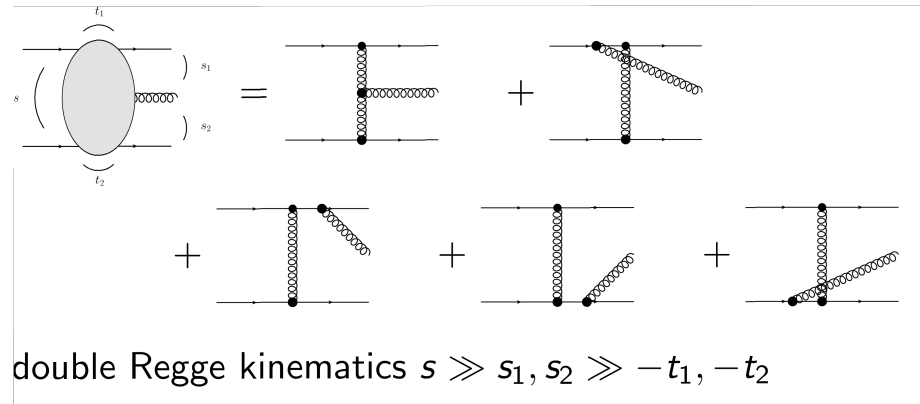
# QCD effective actions at high-energy.

## Are they *really* effective ?

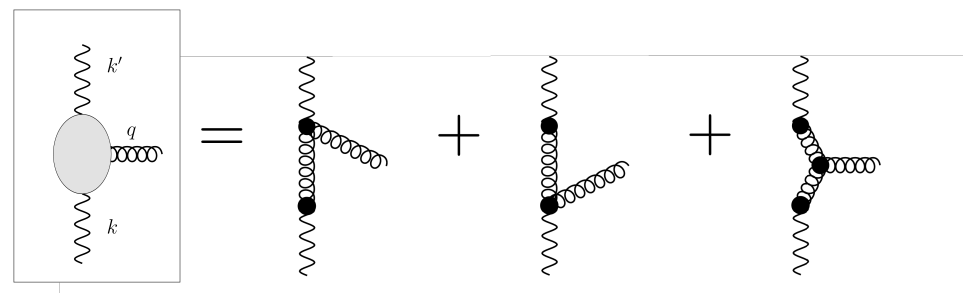
The **Lipatov** action has been constructed in 1995-1997... but **had no application !**

In a nutshell :

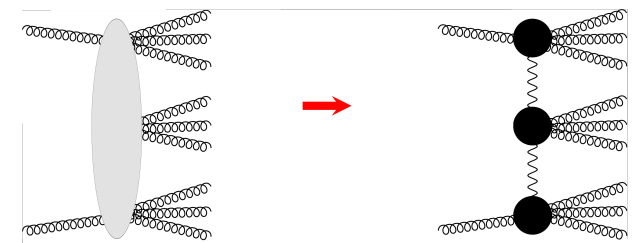
**Lipatov** vertex :  
 combines  
 the QCD triple-vertex +  
 Bremsstrahlung emissions  
 Key point : the emitted gluon is **soft**  
 with respect to the emitter  
 ~ eikonal line



Define two Reggeon fields  $A_+, A_-$   
 which incorporate this eikonal  
 nature, either from upper or  
 lower side, on top of usual  
 QCD gluons



Now iterate : key point = locality in rapidity multiregge  
 (LO) or quasi-multiregge (NLO) kinematics  
 The effective action should be supplemented with  
 additional rules... which makes life hard



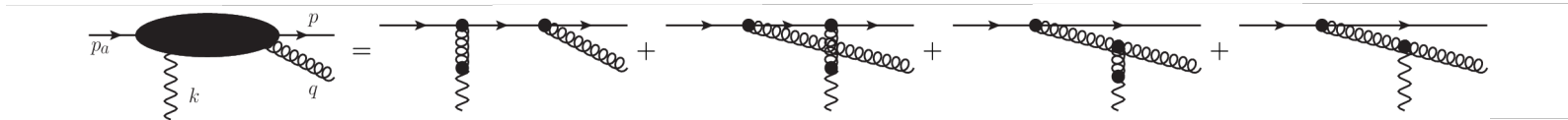
# Yes, the **Lipatov** action can now be used practice. Important progresses have been made recently :

Analytically

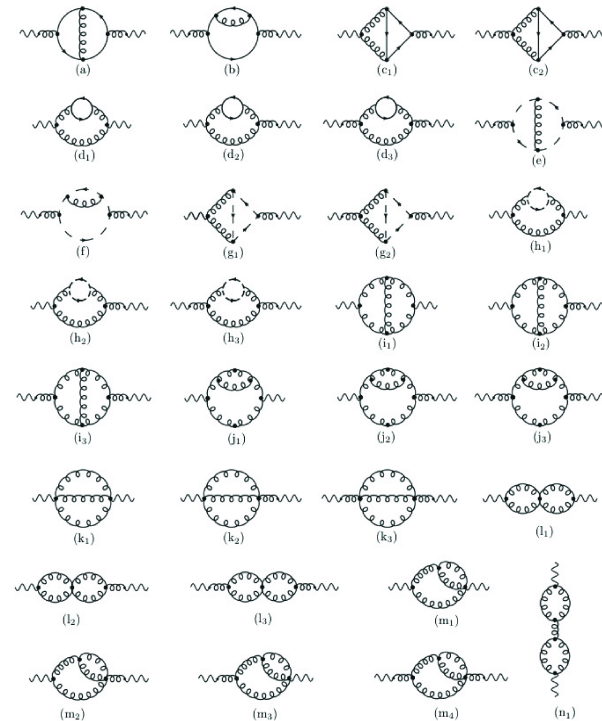
See **Martin Hentschinski** and **Grigorios Chachamis**

Several non trivial results which have been reobtained :

- Quasi-elastic quark vertex at NLO (building block for **Mueller Navelet** jets) = jet vertex

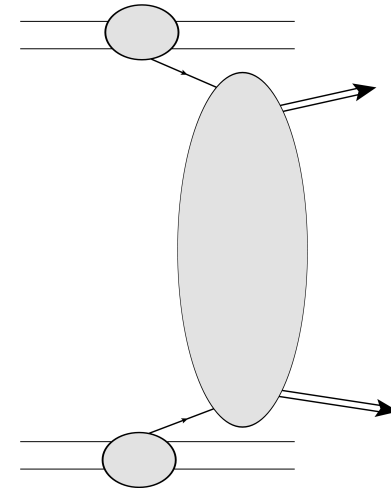


- Two-loop gluon Regge trajectory

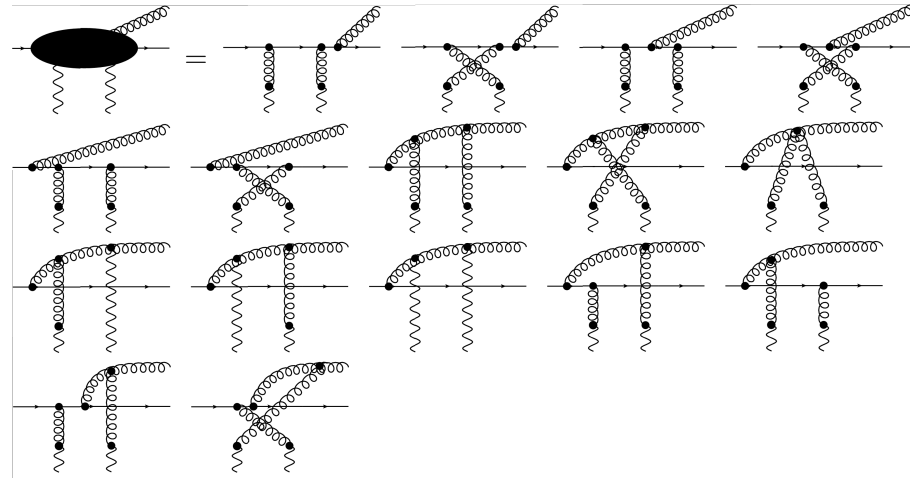


# A new result which have been obtained using the Lipatov action

Forward-backward jets with rapidity gap



Jet vertex at NLO :



# Yes, the Lipatov action can now be used practice. Important progress have been made recently :

## Numerical implementation

See [Handreas Van Hameren](#)

- we are just interested in a gauge invariant amplitude  $\mathcal{A}(g^*g^* \rightarrow X)$
- the amplitude  $\mathcal{A}(q_A q_B \rightarrow q_A q_B + X)$  must be gauge invariant, must be completely on-shell, but does not have to be physical
- introduce complex on-shell momenta  $p_A, p_{A'}, p_B, p_{B'}$

$$\ell_3^\mu = \frac{1}{2} \langle \ell_2 | \gamma^\mu | \ell_1 \rangle$$

$$\ell_4^\mu = \frac{1}{2} \langle \ell_1 | \gamma^\mu | \ell_2 \rangle$$

$$\ell_1^2 = \ell_2^2 = 0$$

$$\ell_3^2 = \ell_4^2 = 0$$

$$\ell_{1,2} \cdot \ell_{3,4} = 0$$

$$\ell_1 \cdot \ell_2 = -\ell_3 \cdot \ell_4$$

$$p_A^\mu = (\Lambda + x_1) \ell_1^\mu - \frac{\ell_4 \cdot k_{1\perp}}{\ell_1 \cdot \ell_2} \ell_3^\mu \quad p_{A'}^\mu = \Lambda \ell_1^\mu + \frac{\ell_3 \cdot k_{1\perp}}{\ell_1 \cdot \ell_2} \ell_4^\mu$$

$$p_B^\mu = (\Lambda + x_2) \ell_2^\mu - \frac{\ell_3 \cdot k_{2\perp}}{\ell_1 \cdot \ell_2} \ell_4^\mu \quad p_{B'}^\mu = \Lambda \ell_2^\mu + \frac{\ell_4 \cdot k_{2\perp}}{\ell_1 \cdot \ell_2} \ell_3^\mu$$

Now we have both the high-energy limit and on-shellness:

$$p_A^\mu - p_{A'}^\mu = x_1 \ell_1^\mu + k_{1\perp}^\mu \quad p_B^\mu - p_{B'}^\mu = x_2 \ell_2^\mu + k_{2\perp}^\mu$$

$$p_A^2 = p_{A'}^2 = p_B^2 = p_{B'}^2 = 0$$

for any value of the dimensionless parameter  $\Lambda$ .

The transverse momenta are now complex. There are replaced by spinors.  
The kinematics is not approximated at that stage.

The obtained rules are equivalent to Lipatov action.

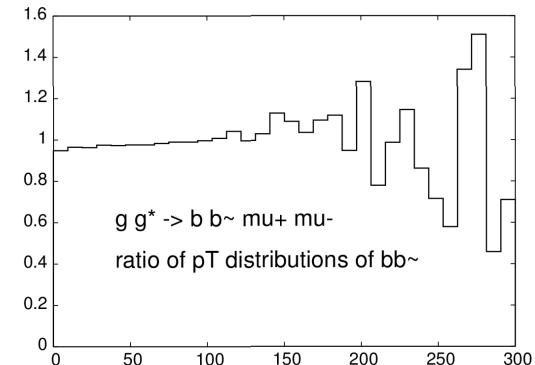
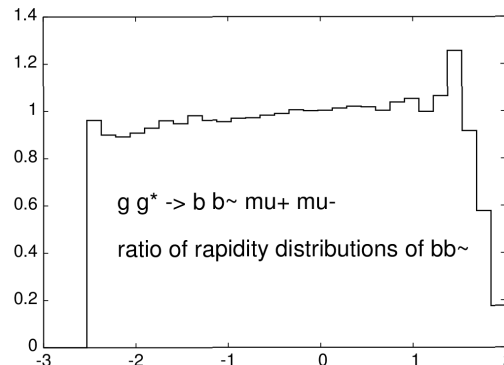
They can be numerically implemented.

# A process computed at tree level based on a numerical implementation of the effective action :

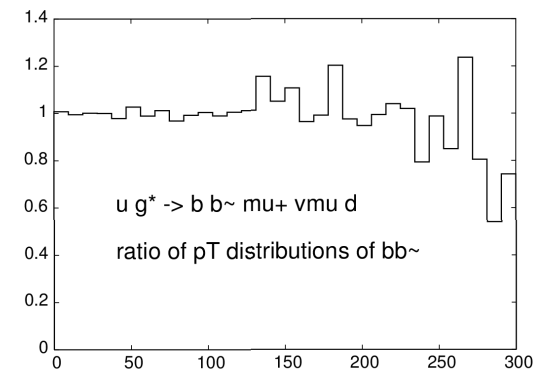
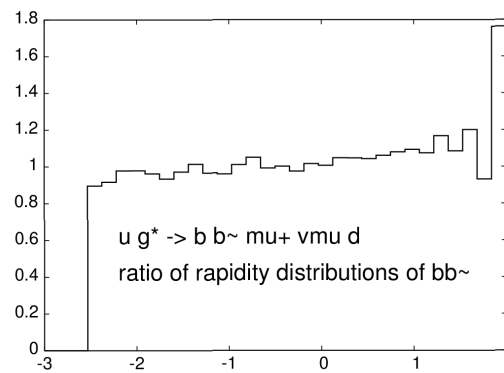
Ratio of observable distributions for p-p vs. p-Pb collisions.

Use unintegrated gluon densities from [Phys.Rev.D86\(2012\)094043](#) for off-shell gluon.

$gg^* \rightarrow b\bar{b} \mu^+ \mu^-$   
 $p_T(q) > 20 \text{ GeV} \quad y(q) < 2.5$   
 $p_T(\mu) > 20 \text{ GeV} \quad y(\mu) < 2.1$   
 $dR(q, q) > 0.4 \quad dR(q, \mu) > 0.4$   
 $\sqrt{s} = 8 \text{ TeV}$



$ug^* \rightarrow b\bar{b} \mu^+ \nu_\mu d$   
 $p_T(q) > 20 \text{ GeV} \quad y(q) < 2.5$   
 $20 \text{ GeV} < p_T(\mu^+) < 50 \text{ GeV}$   
 $y(\mu) < 2.1$   
 $\cancel{E}_T > 20 \text{ GeV}$   
 $dR(q, q) > 0.4 \quad dR(q, \mu) > 0.4$



# The (global) (quasi) conformal symmetry is central for BFKL at LO and NLO

Victor Fadin

## In the singlet channel :

- The full momentum space NLO BFKL kernel (i.e. also the non-forward part of the NLO BFKL kernel) can be obtained from the Möbius form (i.e. dipole, in coordinate space), which is quasi-conformal invariant (i.e. conformal up to the running coupling effect)
- It is then possible to get, in momentum space, the difference between the two forms of the kernel

## In the octet channel :

- There is a similarity which relates the quasi-conformal and the standard BFKL NLO kernel
- The explicit form of this transform has been obtained

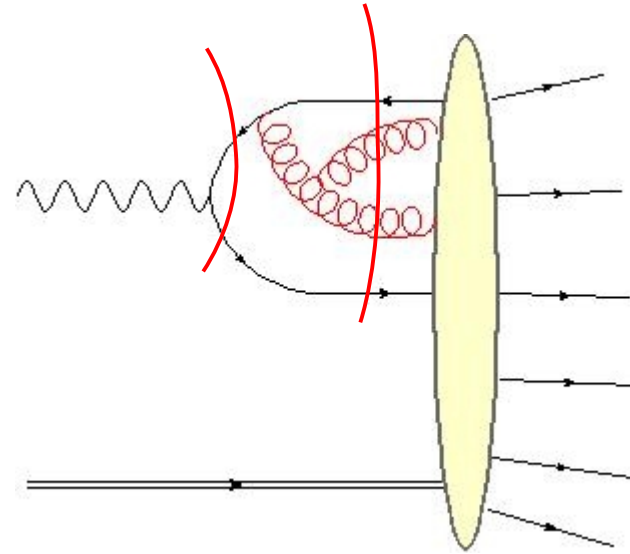


# QCD at high density: How to test it?

**The dipole model** : a key, inspiring and powerful paradigm

At an **electron-hadron collider**:

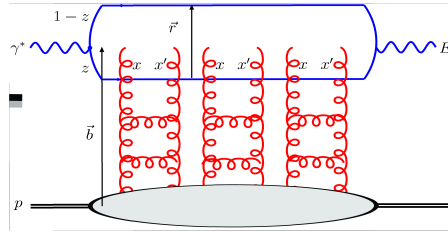
- DIS can be understood as a dipole of “tunable” size  $r$  interacting with the target (p or A), that gets denser at higher energies.
- exclusive final states can be included with an appropriate wave function



A lot of understanding of the dipole scattering amplitude was gained at HERA, at the border of the dense/saturation regime of QCD!

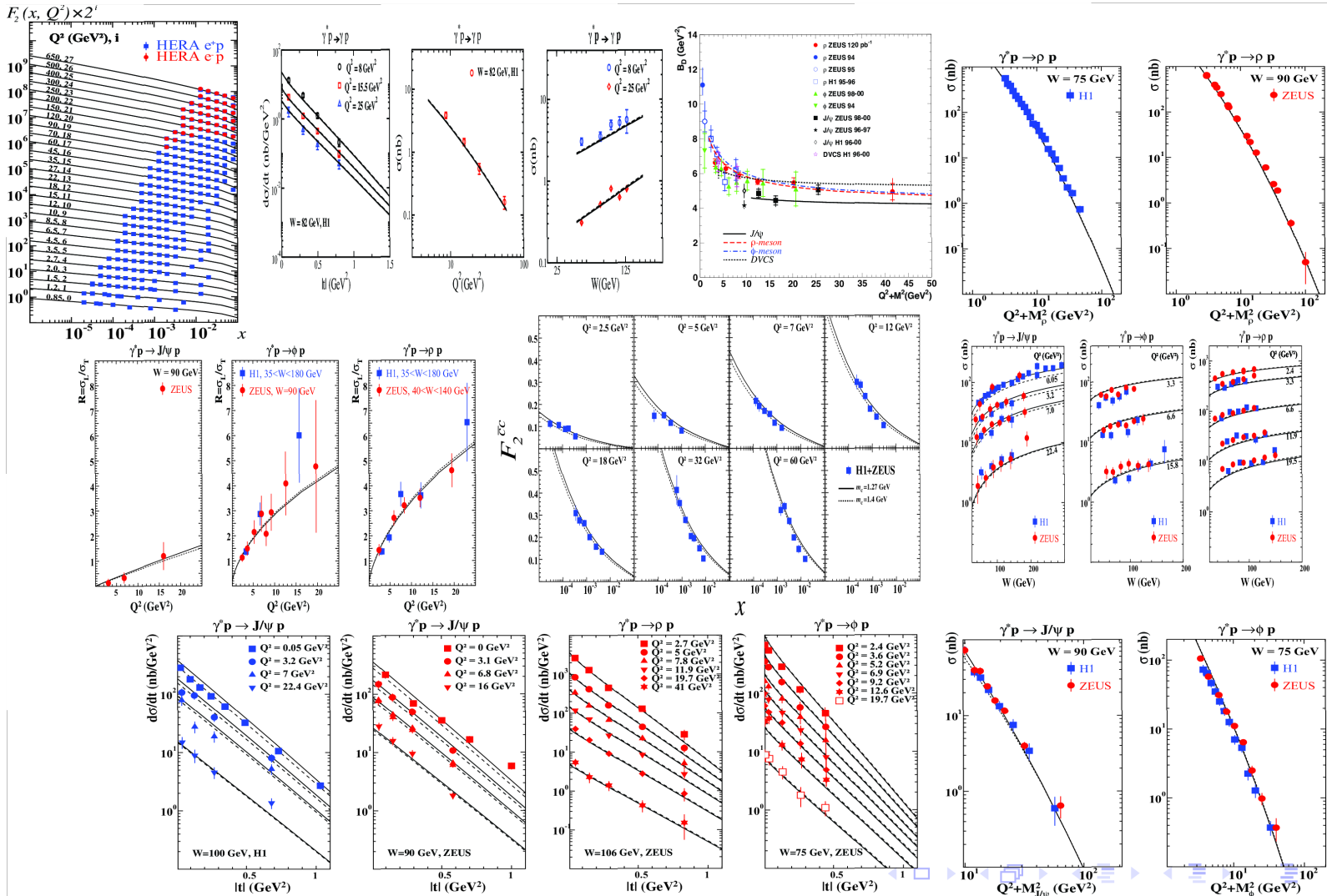
It is “easy” to formulate the QCD evolution of the dipole amplitude with the energy as **radiative corrections to the dipole wave function**.

**BFKL** (at low density), **BK**, **JIMWLK** equations (accounting for high-density effects)

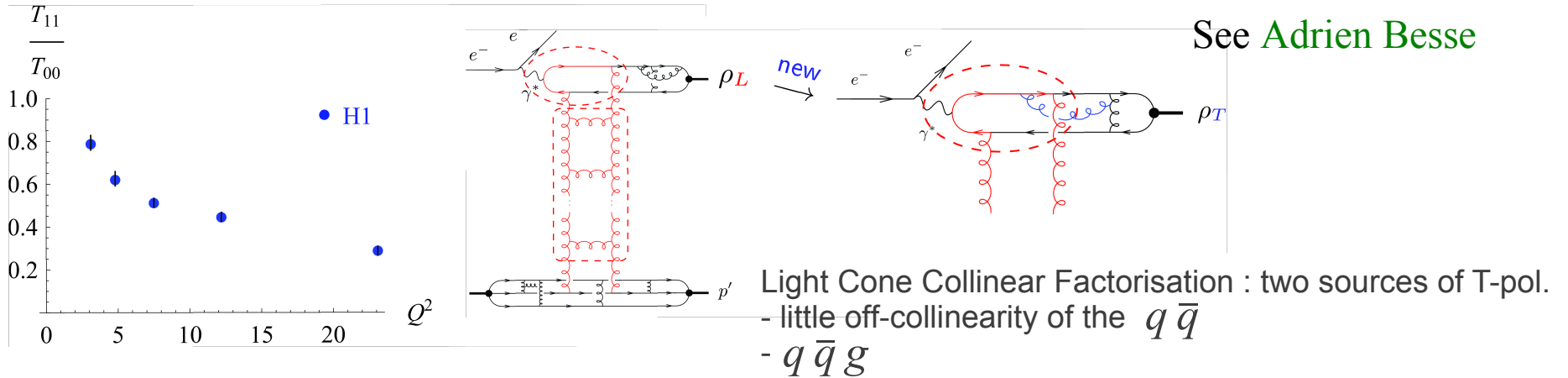


Mueller-Glauber (no small-x dynamics à la BK)  
+ fit for b

→ Unified description of  $x$ ,  $Q^2$ ,  $W$  and  $t$  HERA data



# But what about power corrections in exclusive processes ?

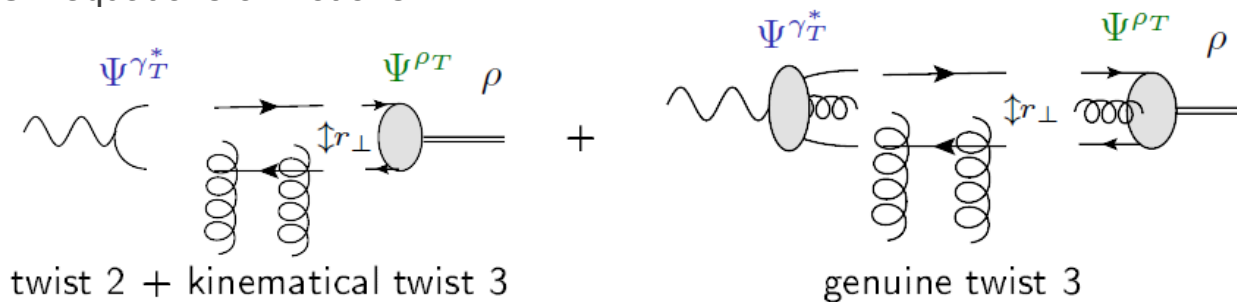


How to combine consistently two mechanisms :

- collinear factorisation to produce a meson **beyond leading twist**
- the dipole QCD at high density

Key ideas :

- Reformulate the Light-Cone Collinear Factorisation in coordinate space
- Use QCD equations of motions



**The dipole is still valid, at finite  $N_c$ , at twist 3**

This provides a way to relate the wave function with the Distribution Amplitude

Wave function = non-perturbative object :

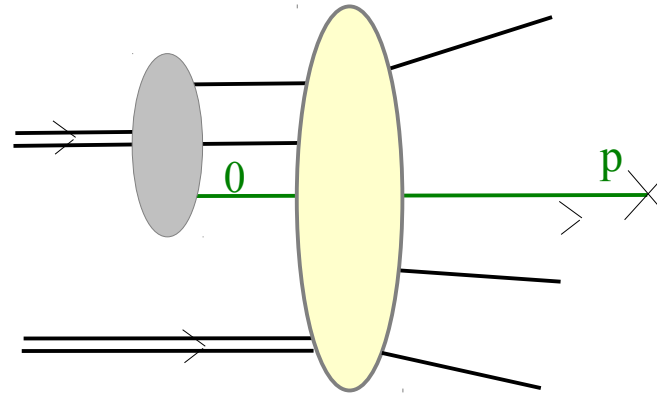
see talk of [Ruben Sandapen](#) for a result based on AdS/QCD correspondence

# QCD at high density: How to test it?

At a **hadron collider**, we need to find appropriate production processes:

★  $p_T$  -broadening:

S. Munier

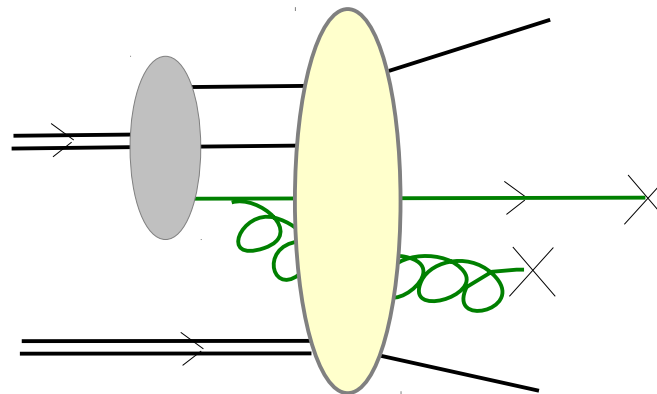


*Observe a jet of transverse momentum*

$$p \sim Q_s$$

★ Forward dijet azimuthal correlations:

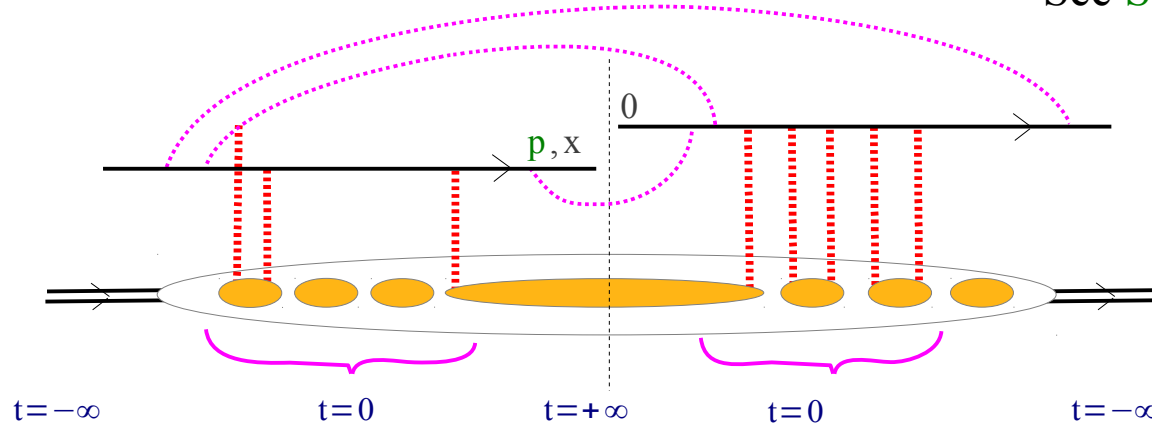
C. Marquet



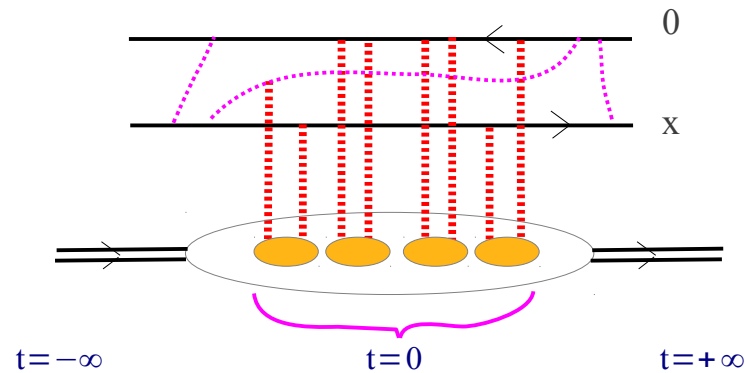
*Observe two forward jets, which are back-to-back if the target is dilute*

# at NLO, pt-broadening = dipole scattering amplitude

See Stéphane Munier



$$\frac{dN}{d^2 \mathbf{p}} = \int \frac{d^2 \mathbf{x}}{(2\pi)^2} e^{-i \mathbf{p} \cdot \mathbf{x}} \left\langle \frac{1}{N_c} \text{Tr} \left( \mathbf{T} V_0^* e^{-i \int d^4 y L_1} \right) \left( \mathbf{T} V_x e^{i \int d^4 y L_1} \right) \right\rangle$$



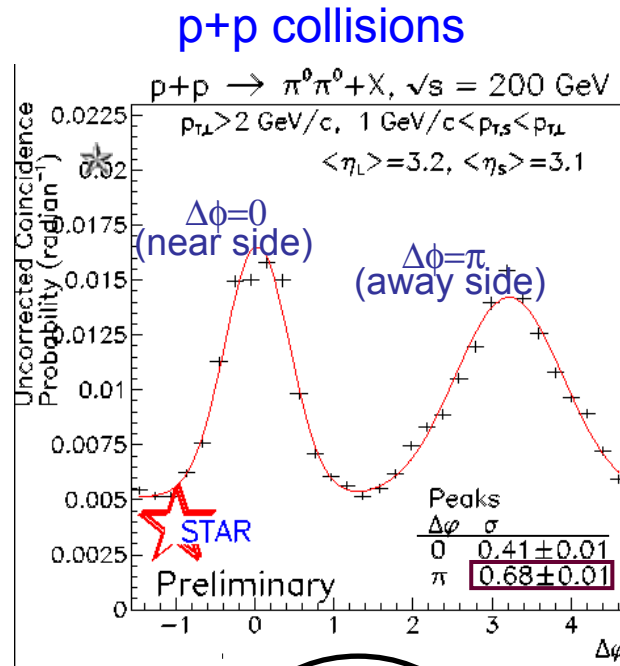
$$S_{\text{dipole}}(\mathbf{x}) = \left\langle \frac{1}{N_c} \text{Tr} \left( \mathbf{T} V_0^* V_x e^{i \int d^4 y L_1} \right) \right\rangle$$

=

# Di-hadron angular correlations as a sign of saturation

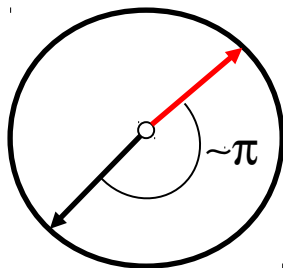
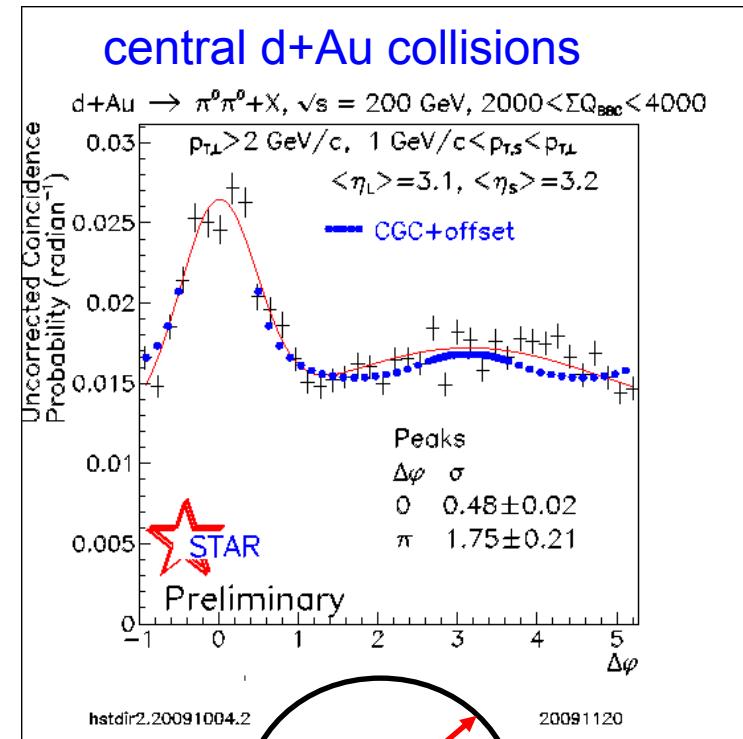
See **Cyrille Marquet**

comparisons between  $d+Au \rightarrow h_1 h_2 X$  (or  $p+Au \rightarrow h_1 h_2 X$ ) and  $p+p \rightarrow h_1 h_2 X$

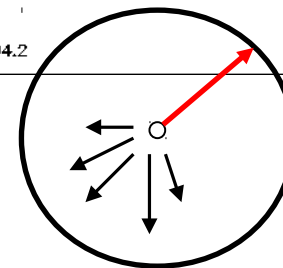


$$\frac{1}{N_{trig}} \frac{dN_{pair}}{d\Delta\phi}$$

Albacete  
and C.Marquet (2010)



$$x_A = \frac{k_1 e^{-y_1} + k_2 e^{-y_2}}{\sqrt{s}} \ll 1$$

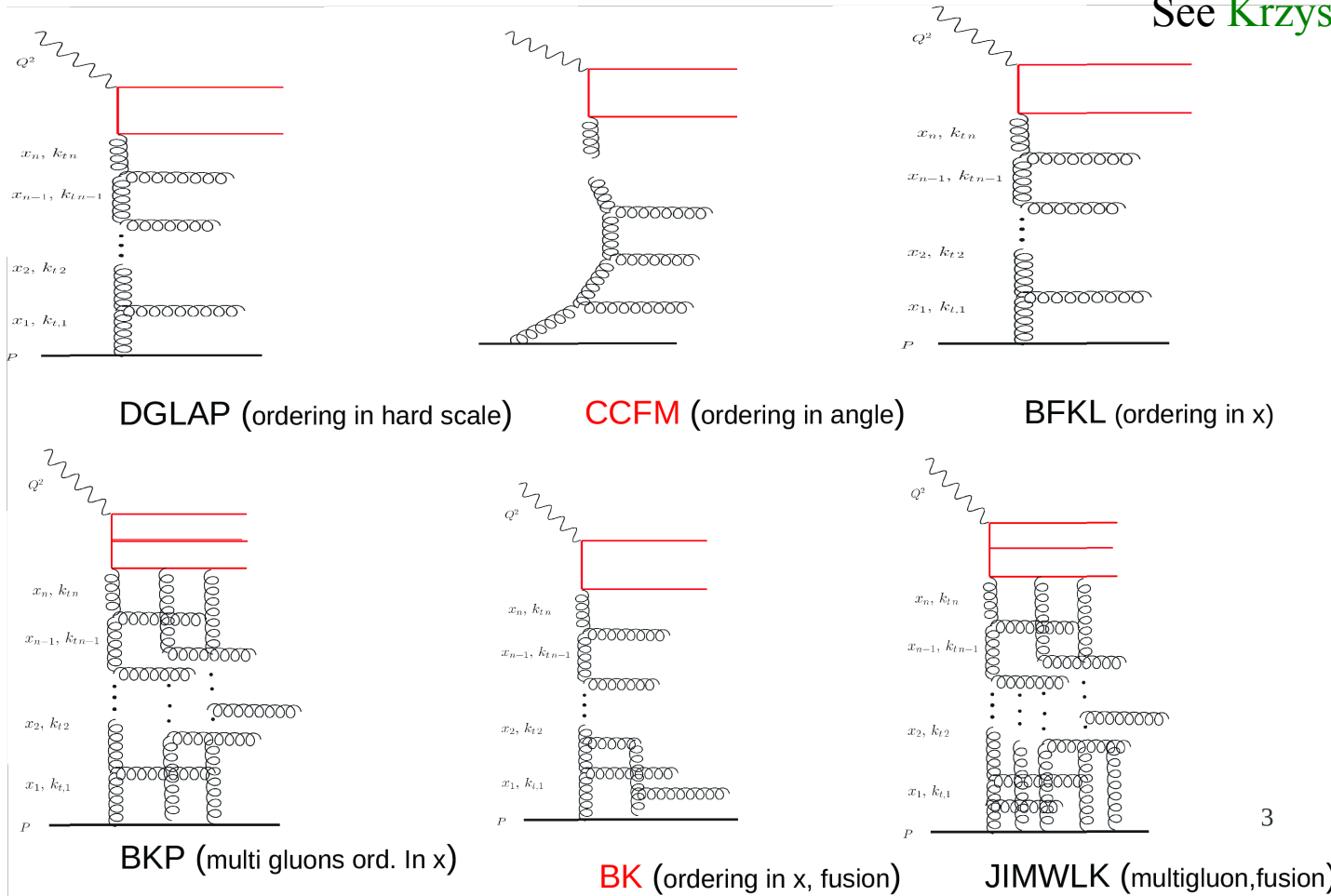


however, when  $y_1 \sim y_2 \sim 0$  (and therefore  $x_A \sim 0.03$ ),  
the p+p and d+Au curves are almost identical

**New :** - dipole and quadrupole contributions are enough in the large  $N_c$  limit  
 - this remains true for multiparticle production

# Exclusive final states and saturation

See [Krzysztof Kutak](#)



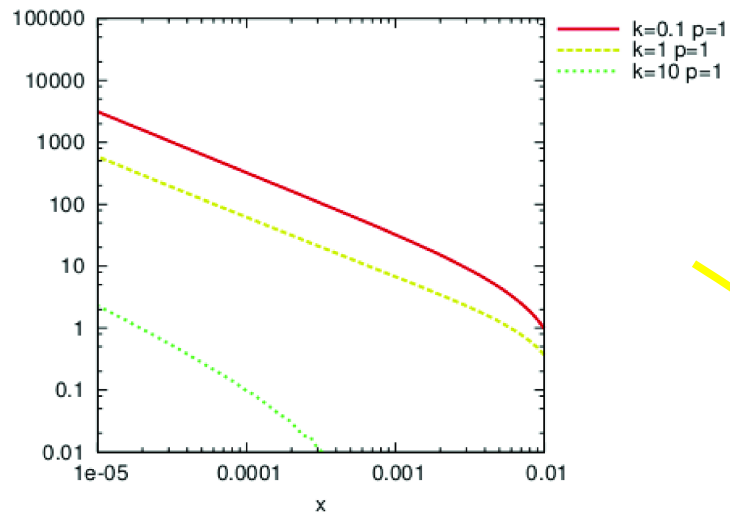
**CCFM + BK**  $\rightarrow$  **KGBJS** equation

Trick : use a resummed form of BK which is more suitable in view of including exclusive final states effects

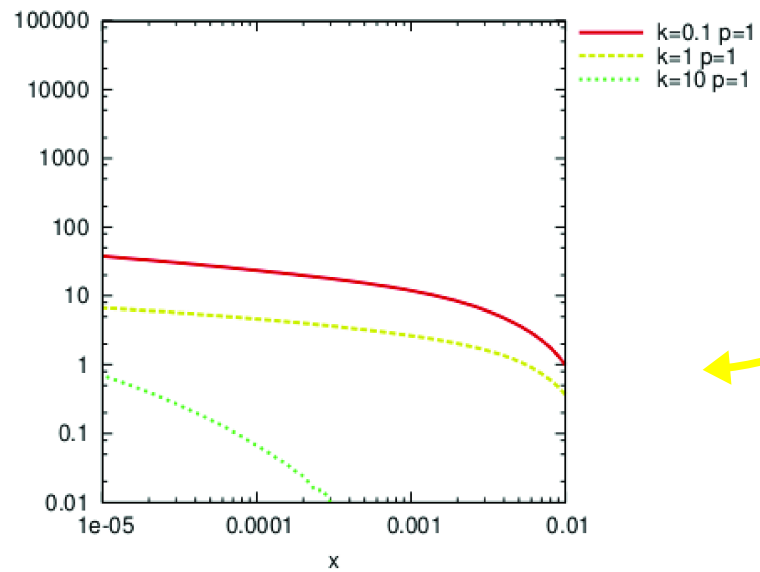
Then postulate ...

(see also the talk of [Michal Deak](#))

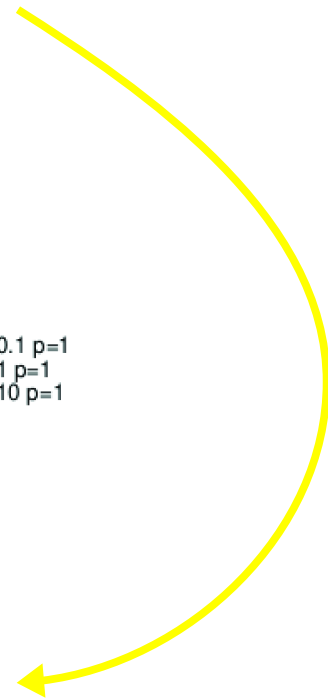
CCFM



KGBJS



low k saturates  
for small x





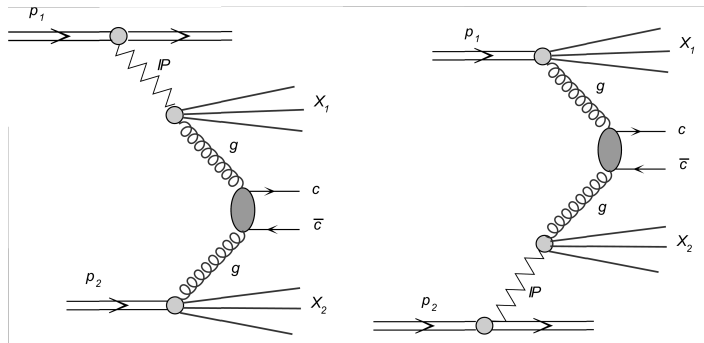
# Testing QCD in the perturbative Regge limit at LHC

One needs an hard scale :

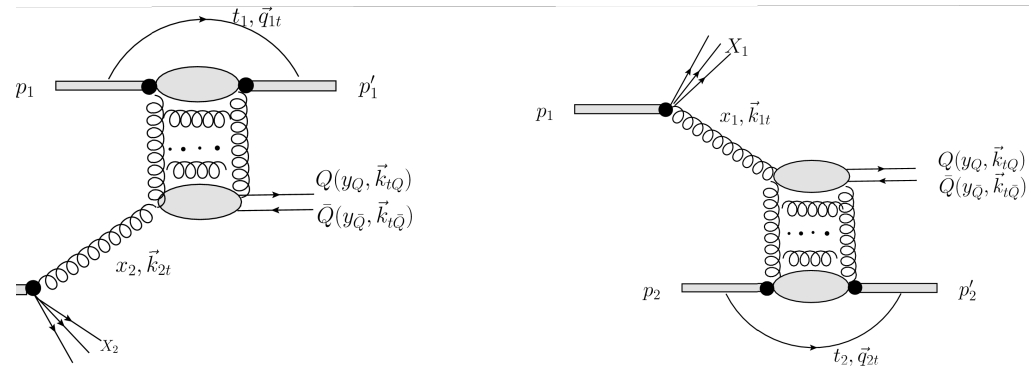
$M_{J/\psi}$  for  $\gamma\gamma \rightarrow J/\psi J/\psi$

in ultraperipheral  $AA \rightarrow AA J/\psi J/\psi$   
 Box diagram versus BFKL ladder ?  
 Wolfgang Schaefer

$M_Q$  for diffractive  $Q\bar{Q}$  production  
 further studies needed : several mechanism are possible  
 Antoni Szczurek

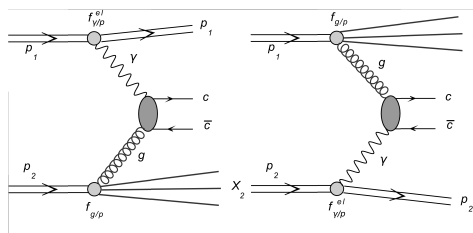


Ingelman-Schlein model  
 dominates



Gluon dissociation

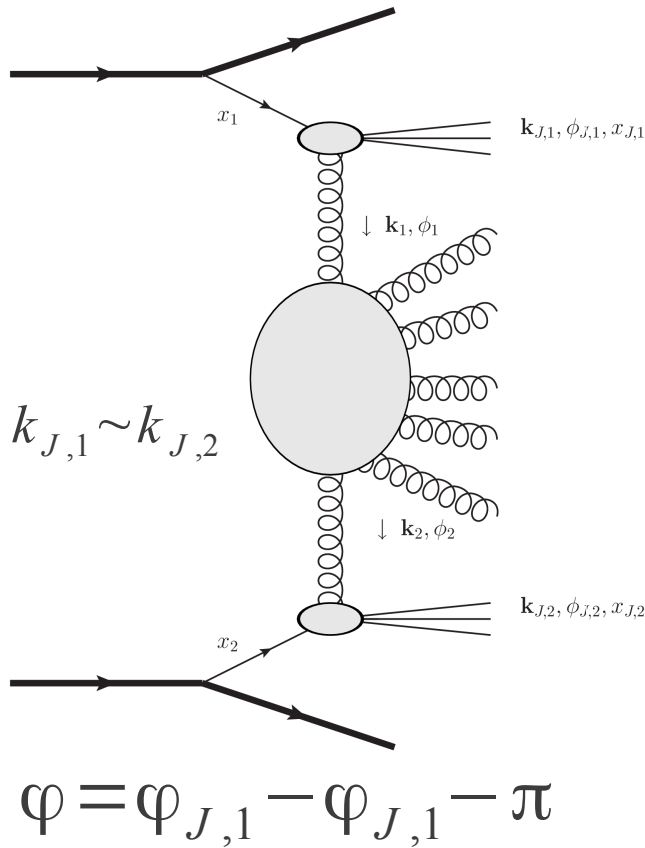
Competitive mechanism :



# Testing QCD in the perturbative Regge limit at LHC

Mueller-Navelet jets : the only observable for which a full NLO BFKL analysis is available

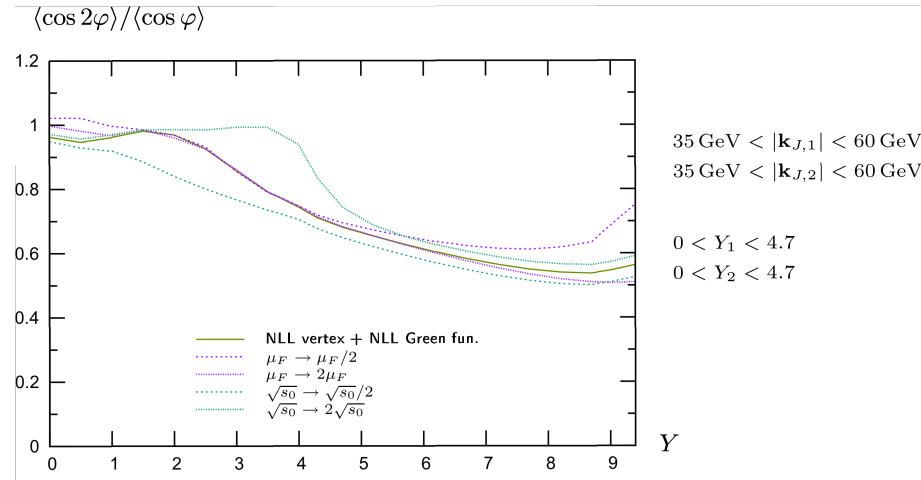
See Bertrand Ducloué



Surprisingly small decorrelation

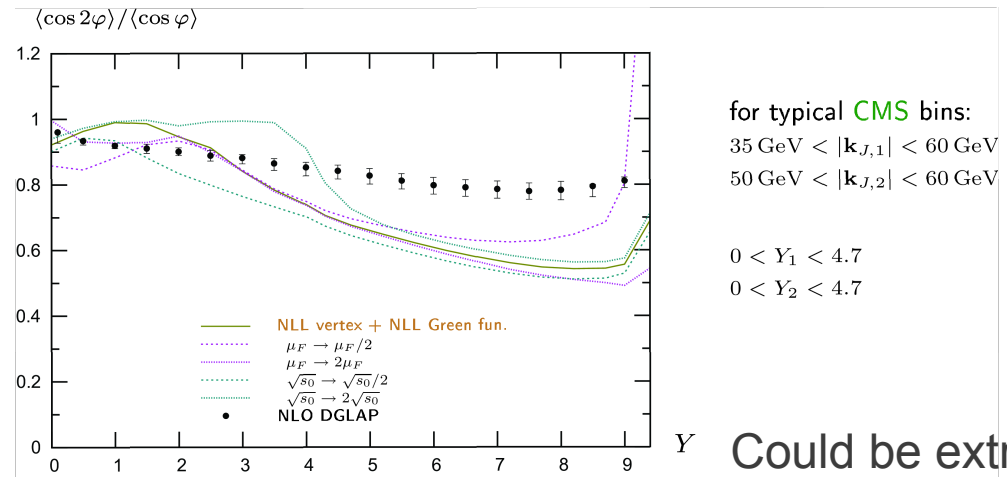
Predictions are stable with respect to

$s_0, \mu_F$ , PDFs, in the range  $4.5 < Y < 8$



Symmetric configuration

See CMS data

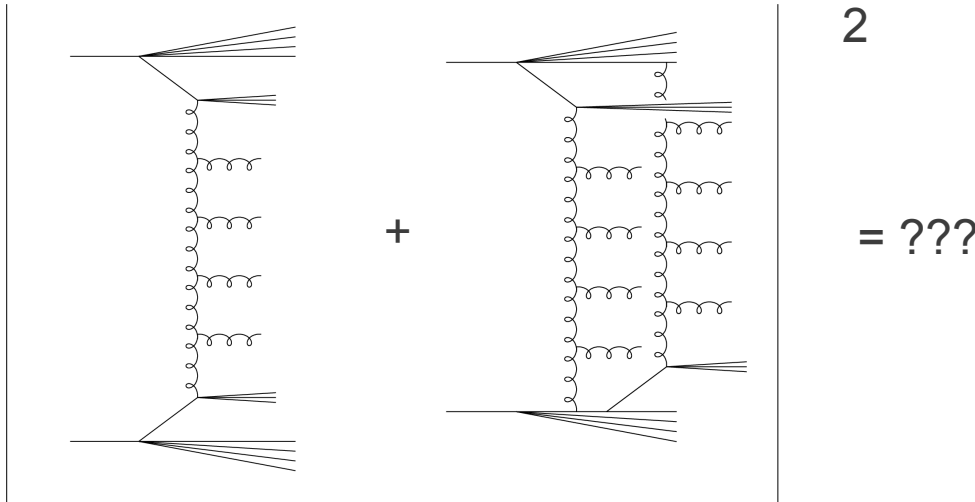


Asymmetric configuration

Could be extracted

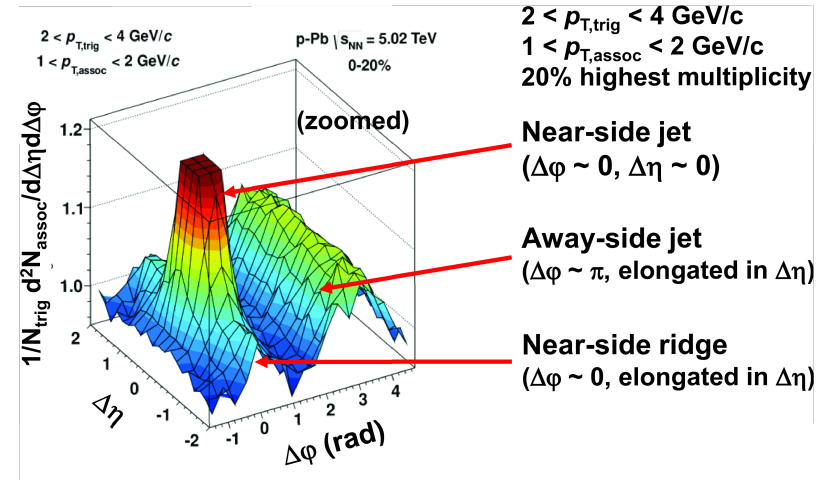
# Testing QCD in the perturbative Regge limit at LHC

Mueller-Navelet jets : another mechanism ?



BFKL ladder

Color Glass Condensate ?  
~ MPI at small x ?



Similar issues for the ridge effect in pp, pA

MPI at medium x : see Talks of Markus Diehl  
 Very few models for double parton distributions  
 Not so easy to satisfy sum rules (see talk of Emilia Lewandowska)