

# Mueller-Navelet Jets at the LHC: Evidence for High-Energy Resummation Effects

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in collaboration with

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D. Colferai, F. Schwennsen, L. Szymanowski, S. W., JHEP 1012 (2010) 026 [arXiv:1002.1365 [hep-ph]]

B. Ducloué, L. Szymanowski, S. W., JHEP 1305 (2013) 096 [arXiv:1302.7012 [hep-ph]]

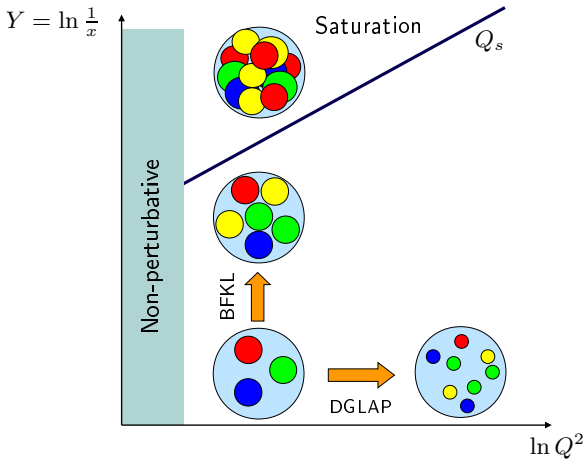
B. Ducloué, L. Szymanowski, S. W., Phys. Rev. Lett. 112 (2014) 082003 [arXiv:1309.3229 [hep-ph]]

B. Ducloué, L. Szymanowski, S. W., Phys. Lett. B 738 (2014) 311-316 [arXiv:1407.6593 [hep-ph]]

B. Ducloué, L. Szymanowski, S. W., arXiv:1507.04735 [hep-ph]

R. Boussarie, B. Ducloué, L. Szymanowski, S. W., *in preparation*

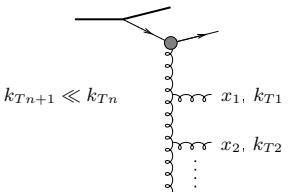
# The different regimes of QCD



# Resummation in QCD: DGLAP vs BFKL

Small values of  $\alpha_s$  (perturbation theory applies if there is a hard scale) can be compensated by large logarithmic enhancements.

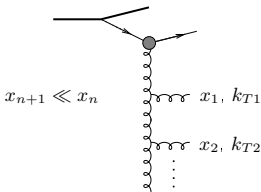
## DGLAP



strong ordering in  $k_T$

$$\sum (\alpha_s \ln Q^2)^n$$

## BFKL



strong ordering in  $x$

$$\sum (\alpha_s \ln s)^n$$

When  $\sqrt{s}$  becomes very large, it is expected that a BFKL description is needed to get accurate predictions

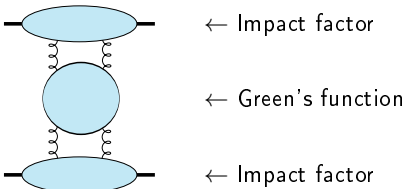
# The specific case of QCD at large $s$

## QCD in the perturbative Regge limit

The amplitude can be written as:

$$\mathcal{A} = \underbrace{\text{Diagram 1}}_{\sim s} + \left( \underbrace{\text{Diagram 2}}_{\sim s(\alpha_s \ln s)} + \underbrace{\text{Diagram 3}}_{\sim s(\alpha_s \ln s)} + \dots \right) + \left( \underbrace{\text{Diagram 4}}_{\sim s(\alpha_s \ln s)^2} + \dots \right) + \dots$$

this can be put in the following form :



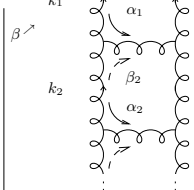
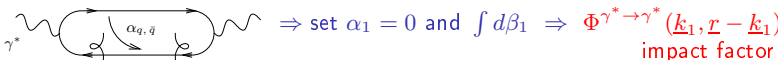
$$\sigma_{tot}^{h_1 h_2 \rightarrow \text{anything}} = \frac{1}{s} \text{Im} \mathcal{A} \sim s^{\alpha_{\mathbb{P}}(0) - 1}$$

with  $\alpha_{\mathbb{P}}(0) - 1 = C \alpha_s + C' \alpha_s^2 + \dots$

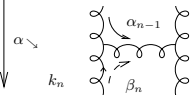
$C > 0$  : Leading Log  $\mathbb{P}$ omeron  
Balitsky, Fadin, Kuraev, Lipatov

# Opening the boxes: Impact representation $\gamma^* \gamma^* \rightarrow \gamma^* \gamma^*$ as an example

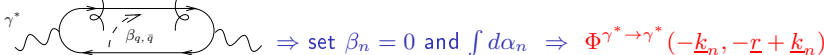
- **Sudakov** decomposition:  $k_i = \alpha_i p_1 + \beta_i p_2 + k_{\perp i}$  ( $p_1^2 = p_2^2 = 0$ ,  $2p_1 \cdot p_2 = s$ )
- write  $d^4 k_i = \frac{s}{2} d\alpha_i d\beta_i d^2 k_{\perp i}$  ( $\underline{k} = \text{Eucl.} \leftrightarrow k_{\perp} = \text{Mink.}$ )
- $t$ -channel gluons have **non-sense** polarizations at large  $s$ :  $\epsilon_{NS}^{up/down} = \frac{2}{s} p_{2/1}$



$$\mathcal{M} = \frac{is}{(2\pi)^2} \int \frac{d^2 \underline{k}}{\underline{k}^2} \Phi^{up}(\underline{k}, \underline{r} - \underline{k}) \int \frac{d^2 \underline{k}'}{\underline{k}'^2} \Phi^{down}(-\underline{k}', -\underline{r} + \underline{k}') \\ \times \int_{\delta - i\infty}^{\delta + i\infty} \frac{d\omega}{2\pi i} \left(\frac{s}{s_0}\right)^\omega G_\omega(\underline{k}, \underline{k}', \underline{r})$$



← multi-Regge kinematics



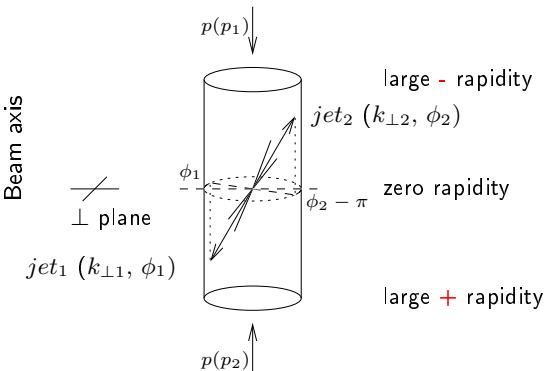
## Higher order corrections

- Higher order corrections to BFKL kernel are known at NLL order (Lipatov Fadin; Camici, Ciafaloni), now for arbitrary impact parameter  $\alpha_S \sum_n (\alpha_S \ln s)^n$  resummation
- impact factors are known in some cases at NLL
  - $\gamma^* \rightarrow \gamma^*$  at  $t = 0$  (Bartels, Colferai, Gieseke, Kyrieleis, Qiao; Balitski, Chirilli)
  - forward jet production (Bartels, Colferai, Vacca; Caporale, Ivanov, Murdaca, Papa, Perri; Chachamis, Hentschinski, Madrigal, Sabio Vera)
  - inclusive production of a pair of hadrons separated by a large interval of rapidity (Ivanov, Papa)
  - $\gamma_L^* \rightarrow \rho_L$  in the forward limit (Ivanov, Kotsky, Papa)

# Mueller-Navelet jets: Basics

## Mueller-Navelet jets

- Consider two jets (hadrons flying within a narrow cone) **separated by a large rapidity**, i.e. each of them almost fly in the direction of the hadron “close” to it, and with very similar transverse momenta
- Pure LO *collinear* treatment: these two jets should be emitted **back to back** at leading order:  $\Delta\phi - \pi = 0$  ( $\Delta\phi = \phi_1 - \phi_2 =$  relative azimuthal angle) and  $k_{\perp 1} = k_{\perp 2}$ . No phase space for (untagged) emission between them



## Master formulas

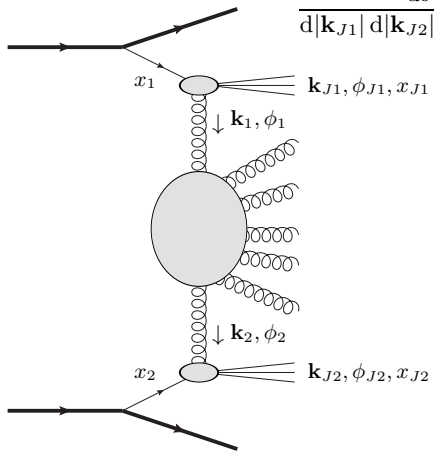
 $k_T$ -factorized differential cross section

$$\frac{d\sigma}{d|\mathbf{k}_{J1}| d|\mathbf{k}_{J2}| dy_{J1} dy_{J2}} = \int d\phi_{J1} d\phi_{J2} \int d^2\mathbf{k}_1 d^2\mathbf{k}_2$$

$$\times \Phi(\mathbf{k}_{J1}, x_{J1}, -\mathbf{k}_1)$$

$$\times G(\mathbf{k}_1, \mathbf{k}_2, \hat{s})$$

$$\times \Phi(\mathbf{k}_{J2}, x_{J2}, \mathbf{k}_2)$$



$$\text{with } \Phi(\mathbf{k}_{J2}, x_{J2}, \mathbf{k}_2) = \int dx_2 f(x_2) V(\mathbf{k}_2, x_2)$$

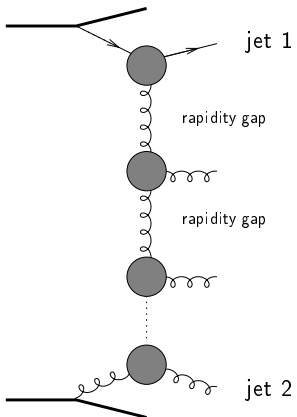
$$f \equiv \text{PDF}$$

$$x_J = \frac{|\mathbf{k}_J|}{\sqrt{s}} e^{y_J}$$



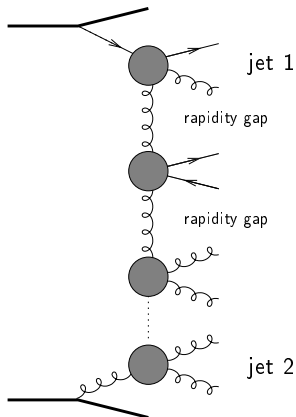
# Mueller-Navelet jets: LL vs NLL

LL BFKL



$$\sum(\alpha_s \ln s)^n$$

NLL BFKL



$$\sum(\alpha_s \ln s)^n + \alpha_s \sum(\alpha_s \ln s)^n$$

# Results

## Results for a symmetric configuration

In the following we show results for

- $\sqrt{s} = 7 \text{ TeV}$
- $35 \text{ GeV} < |\mathbf{k}_{J1}|, |\mathbf{k}_{J2}| < 60 \text{ GeV}$
- $0 < |y_1|, |y_2| < 4.7$

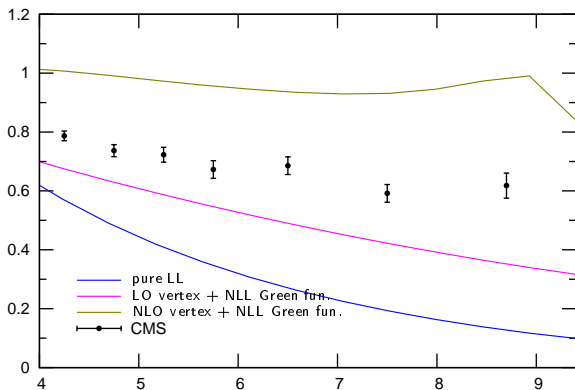
These cuts allow us to compare our predictions with the first experimental data on azimuthal correlations of **Mueller-Navelet** jets at the LHC presented by the **CMS** collaboration (CMS-PAS-FSQ-12-002)

note: unlike experiments we have to set an upper cut on  $|\mathbf{k}_{J1}|$  and  $|\mathbf{k}_{J2}|$ . We have checked that our results do not depend on this cut significantly.

## Results: azimuthal correlations

Azimuthal correlation  $\langle \cos \varphi \rangle$ 

$$\frac{c_1}{c_0} = \langle \cos \varphi \rangle \equiv \langle \cos(\phi_{J1} - \phi_{J2} - \pi) \rangle$$


 $35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$ 
 $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$ 
 $0 < |y_1| < 4.7$ 
 $0 < |y_2| < 4.7$ 
 $Y \equiv |y_1 - y_2|$ 

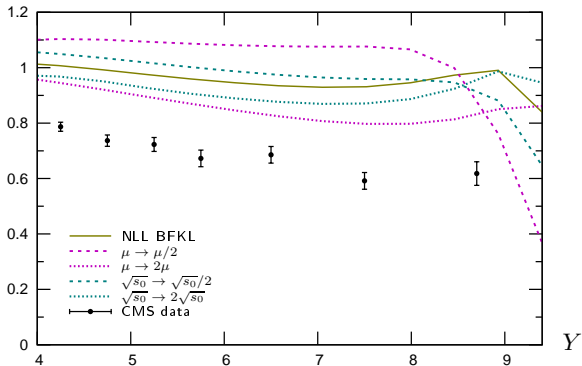
The NLO corrections to the jet vertex lead to a large increase of the correlation

Note: LO vertex + NLL Green done by F. Schwennsen, A. Sabio-Vera; C. Marquet, C. Royon

## Results: azimuthal correlations

Azimuthal correlation  $\langle \cos \varphi \rangle$ 

$$\langle \cos \varphi \rangle \equiv \langle \cos(\phi_{J1} - \phi_{J2} - \pi) \rangle$$



$$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$$

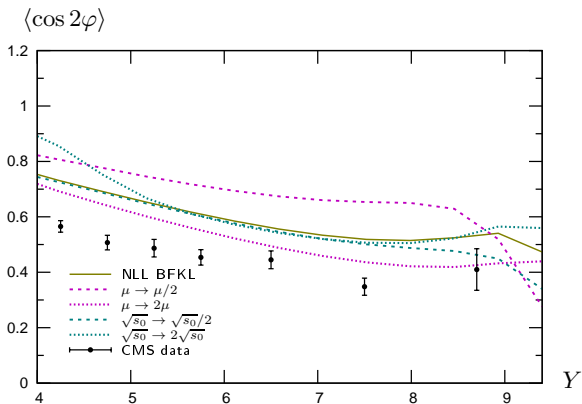
$$35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$$

$$0 < |y_1| < 4.7$$

$$0 < |y_2| < 4.7$$

- NLL BFKL predicts a too small decorrelation
- The NLL BFKL calculation is still rather dependent on the scales, especially the renormalization / factorization scale

## Results: azimuthal correlations

Azimuthal correlation  $\langle \cos 2\varphi \rangle$ 

$$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$$

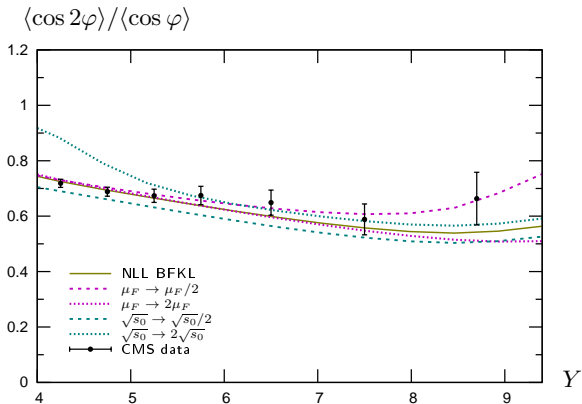
$$35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$$

$$0 < |y_1| < 4.7$$

$$0 < |y_2| < 4.7$$

- The agreement with data is a little better for  $\langle \cos 2\varphi \rangle$  but still not very good
- This observable is also very sensitive to the scales

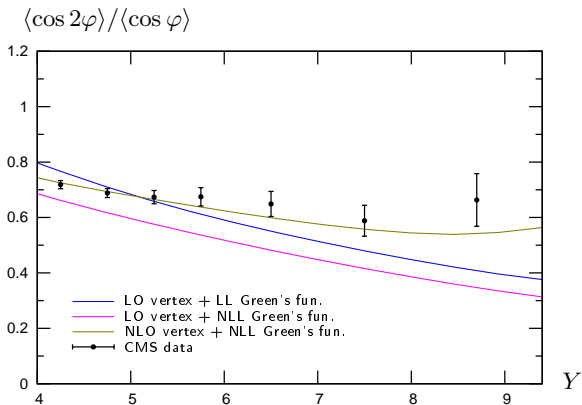
## Results: azimuthal correlations

Azimuthal correlation  $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$  $35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$  $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$  $0 < |y_1| < 4.7$  $0 < |y_2| < 4.7$ 

- This observable is more stable with respect to the scales than the previous ones
- The agreement with data is good across the whole  $Y$  range

# Results: azimuthal correlations

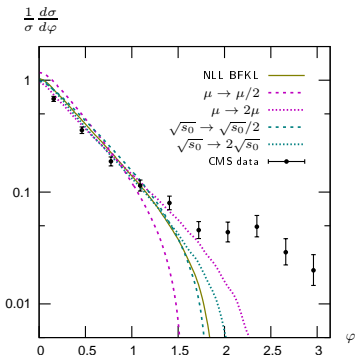
Azimuthal correlation  $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$



$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$   
 $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$   
 $0 < |y_1| < 4.7$   
 $0 < |y_2| < 4.7$

It is necessary to include the NLO corrections to the jet vertex to reproduce the behavior of the data at large  $Y$

## Results: azimuthal distribution

Azimuthal distribution (integrated over  $6 < Y < 9.4$ )

$$\frac{1}{\sigma} \frac{d\sigma}{d\varphi} = \frac{1}{2\pi} \left\{ 1 + 2 \sum_{n=1}^{\infty} \cos(n\varphi) \langle \cos(n\varphi) \rangle \right\}.$$

- Our calculation predicts a too large value of  $\frac{1}{\sigma} \frac{d\sigma}{d\varphi}$  for  $\varphi \lesssim \frac{\pi}{2}$  and a too small value for  $\varphi \gtrsim \frac{\pi}{2}$
- It is not possible to describe the data even when varying the scales by a factor of 2



## Results: limitations

- The agreement of our calculation with the data for  $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$  is good and quite stable with respect to the scales
- The agreement for  $\langle \cos n\varphi \rangle$  and  $\frac{1}{\sigma} \frac{d\sigma}{d\varphi}$  is not very good and very sensitive to the choice of the renormalization scale  $\mu_R$
- An all-order calculation would be independent of the choice of  $\mu_R$ . This feature is lost if we truncate the perturbative series  
 ⇒ How to choose the renormalization scale?  
 'Natural scale': sometimes the typical momenta in a loop diagram are different from the natural scale of the process

We decided to use the **Brody-Lepage-Mackenzie (BLM)** procedure to fix the renormalization scale

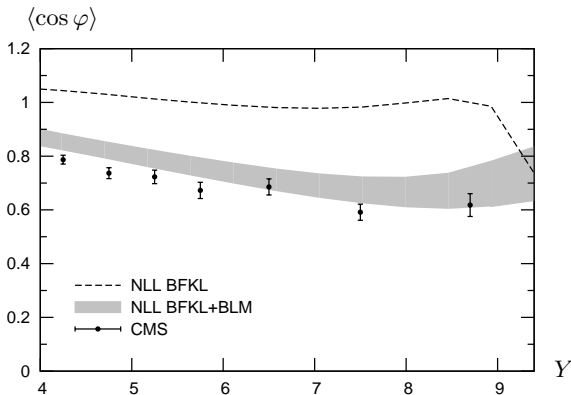
## The BLM renormalization scale fixing procedure

The **Brodsky-Lepage-Mackenzie (BLM)** procedure resums the self-energy corrections to the gluon propagator at one loop into the running coupling.

First attempts to apply BLM scale fixing to BFKL processes lead to problematic results. **Brodsky, Fadin, Kim, Lipatov and Pivovarov** suggested that one should first go to a physical renormalization scheme like MOM and then apply the 'traditional' BLM procedure, i.e. identify the  $\beta_0$  dependent part and choose  $\mu_R$  such that it vanishes.

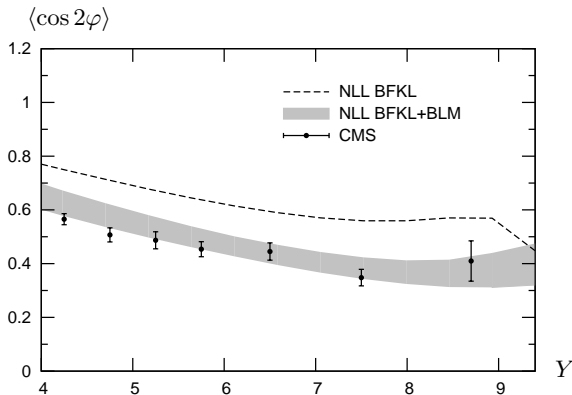
We followed this prescription for the full amplitude at NLL.

## Results with BLM

Azimuthal correlation  $\langle \cos \varphi \rangle$ 
 $35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$ 
 $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$ 
 $0 < |y_1| < 4.7$ 
 $0 < |y_2| < 4.7$ 

Using the BLM scale setting, the agreement with data becomes much better

## Results with BLM

Azimuthal correlation  $\langle \cos 2\varphi \rangle$ 

$$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$$

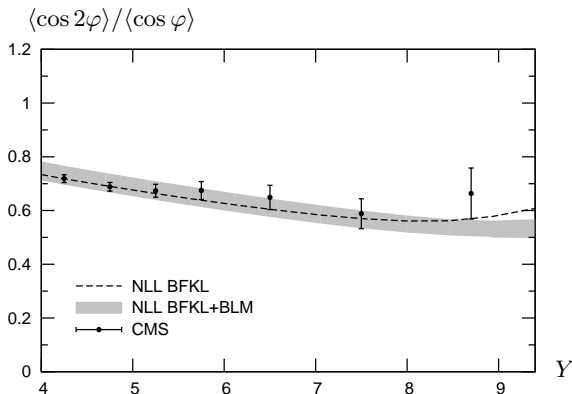
$$35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$$

$$0 < |y_1| < 4.7$$

$$0 < |y_2| < 4.7$$

Using the BLM scale setting, the agreement with data becomes much better.

## Results with BLM

Azimuthal correlation  $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$ 

$$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$$

$$35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$$

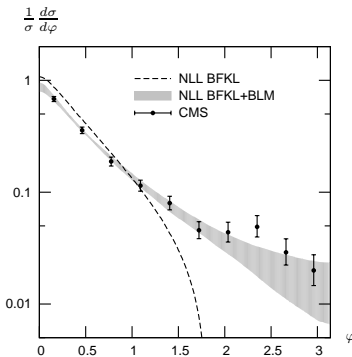
$$0 < |y_1| < 4.7$$

$$0 < |y_2| < 4.7$$

Because it is much less dependent on the scales, the observable  $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$  is almost not affected by the BLM procedure and is still in good agreement with the data.

## Results with BLM

Azimuthal distribution (integrated over  $6 < Y < 9.4$ )



With the BLM scale setting the azimuthal distribution is in good agreement with the data across the full  $\varphi$  range.

## Comparison with fixed-order

Using the **BLM** scale setting:

- The agreement  $\langle \cos n\varphi \rangle$  with the data becomes much better
- The agreement for  $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$  is still good and unchanged as this observable is weakly dependent on  $\mu_R$
- The azimuthal distribution is in much better agreement with the data

But the configuration chosen by **CMS** with  $\mathbf{k}_{J_{\min 1}} = \mathbf{k}_{J_{\min 2}}$  does not allow us to compare with a **fixed-order**  $\mathcal{O}(\alpha_s^3)$  treatment (i.e. without resummation)

- These calculations are unstable when  $\mathbf{k}_{J_{\min 1}} = \mathbf{k}_{J_{\min 2}}$  because the cancellation of some divergencies is difficult to obtain numerically
  - Presumably, resummation effects à la **Sudakov** could be important in the limit  $\mathbf{k}_{J_1} \simeq \mathbf{k}_{J_2}$  and require a special treatment
- Work in progress in collaboration with **A. H. Mueller, B-W. Xiao, F. Yuan**

# Comparison with fixed-order

## Results for an asymmetric configuration

In this section we choose the cuts as

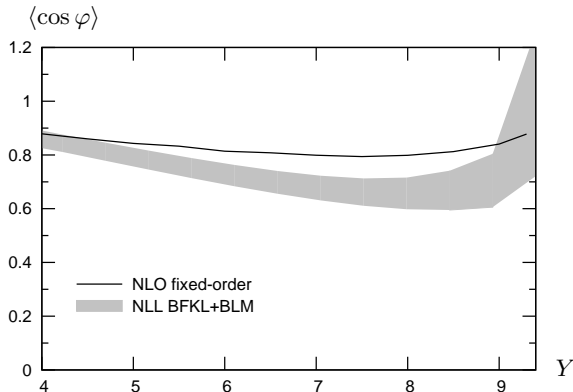
- $35 \text{ GeV} < |\mathbf{k}_{J1}|, |\mathbf{k}_{J2}| < 60 \text{ GeV}$
- $50 \text{ GeV} < \text{Max}(|\mathbf{k}_{J1}|, |\mathbf{k}_{J2}|)$
- $0 < |y_1|, |y_2| < 4.7$

and we compare our results with the NLO fixed-order code Dijet ([Aurenche, Basu, Fontannaz](#)) in the same configuration



# Comparison with fixed-order

## Azimuthal correlation $\langle \cos \varphi \rangle$

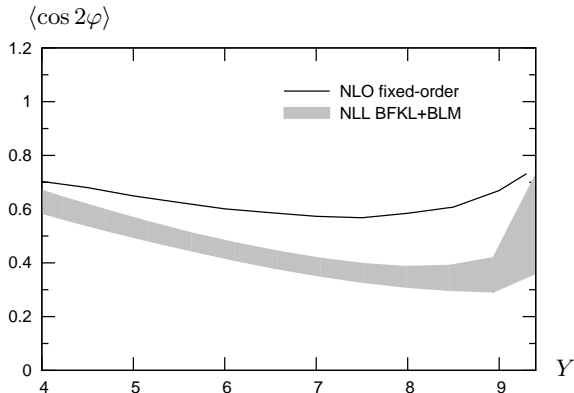


$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$   
 $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$   
 $50 \text{ GeV} < \text{Max}(|\mathbf{k}_{J1}|, |\mathbf{k}_{J2}|)$   
 $0 < |y_1| < 4.7$   
 $0 < |y_2| < 4.7$

The NLO fixed-order and NLL BFKL+BLM calculations are very close

# Comparison with fixed-order

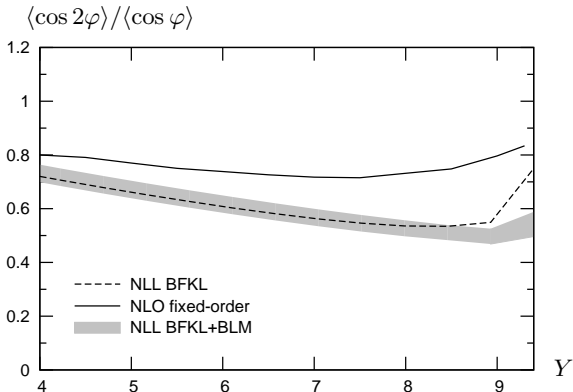
## Azimuthal correlation $\langle \cos 2\varphi \rangle$



$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$   
 $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$   
 $50 \text{ GeV} < \text{Max}(|\mathbf{k}_{J1}|, |\mathbf{k}_{J2}|)$   
 $0 < |y_1| < 4.7$   
 $0 < |y_2| < 4.7$

The BLM procedure leads to a sizable difference between NLO fixed-order and NLL BFKL+BLM.

## Comparison with fixed-order

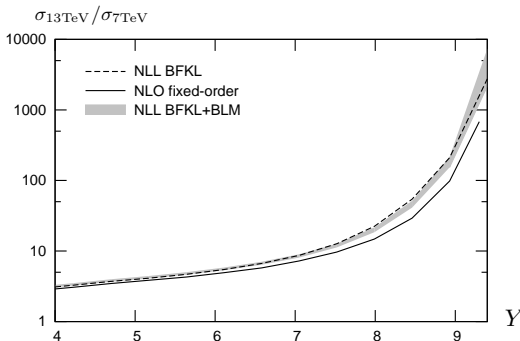
Azimuthal correlation  $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$ 

$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$   
 $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$   
 $50 \text{ GeV} < \text{Max}(|\mathbf{k}_{J1}|, |\mathbf{k}_{J2}|)$   
 $0 < |y_1| < 4.7$   
 $0 < |y_2| < 4.7$

Using **BLM** or not, there is a **sizable difference** between **BFKL** and fixed-order.

# Comparison with fixed-order

Cross section: 13 TeV vs. 7 TeV



$$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$$

$$35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$$

$$50 \text{ GeV} < \text{Max}(|\mathbf{k}_{J1}|, |\mathbf{k}_{J2}|)$$

$$0 < |y_1| < 4.7$$

$$0 < |y_2| < 4.7$$

- In a **BFKL** treatment, a **strong rise of the cross section with increasing energy** is expected.
- This rise is faster than in a fixed-order treatment

## Energy-momentum conservation

- It is necessary to have  $\mathbf{k}_{J_{\min 1}} \neq \mathbf{k}_{J_{\min 2}}$  for comparison with fixed order calculations but this can be problematic for **BFKL** because of energy-momentum conservation
- There is no strict energy-momentum conservation in **BFKL**
- This was studied at LO by **Del Duca and Schmidt**. They introduced an effective rapidity  $Y_{\text{eff}}$  defined as

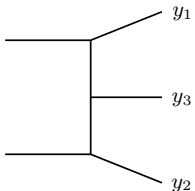
$$Y_{\text{eff}} \equiv Y \frac{\sigma^{2 \rightarrow 3}}{\sigma^{\text{BFKL}, \mathcal{O}(\alpha_s^3)}}$$

- When one replaces  $Y$  by  $Y_{\text{eff}}$  in the expression of  $\sigma^{\text{BFKL}}$  and truncates to  $\mathcal{O}(\alpha_s^3)$ , the exact  $2 \rightarrow 3$  result is obtained

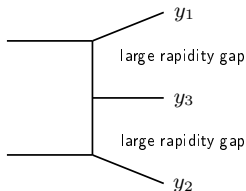
# Energy-momentum conservation

We follow the idea of [Del Duca and Schmidt](#), adding the NLO jet vertex contribution:

exact  $2 \rightarrow 3$

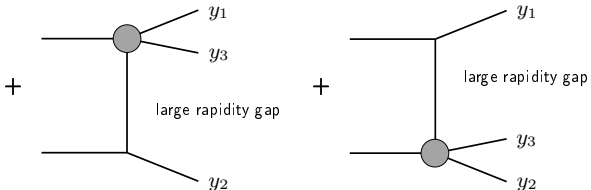


BFKL



one emission from the Green's function + LO jet vertex

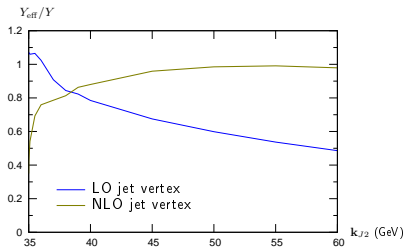
we have to take into account these additional  $\mathcal{O}(\alpha_s^3)$  contributions:



no emission from the Green's function + NLO jet vertex

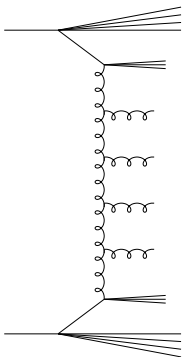
# Energy-momentum conservation

Variation of  $Y_{\text{eff}}/Y$  as a function of  $k_{J2}$  for fixed  $k_{J1} = 35$  GeV (with  $\sqrt{s} = 7$  TeV,  $Y = 8$ ):



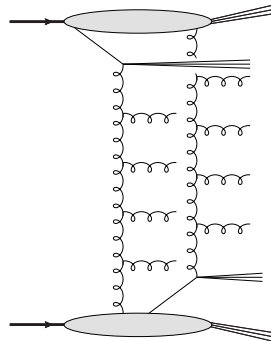
- With the **LO** jet vertex,  $Y_{\text{eff}}$  is much smaller than  $Y$  when  $k_{J1}$  and  $k_{J2}$  are significantly different
- This is the region important for comparison with fixed order calculations
- The improvement coming from the **NLO** jet vertex is very large in this region
- For  $k_{J1} = 35$  GeV and  $k_{J2} = 50$  GeV, typical of the values we used for comparison with fixed order, we get  $\frac{Y_{\text{eff}}}{Y} \simeq 0.98$  at NLO vs.  $\sim 0.6$  at LO

# Can Mueller-Navelet jets be a manifestation of multiparton interactions?



MN jets in the single partonic model

+

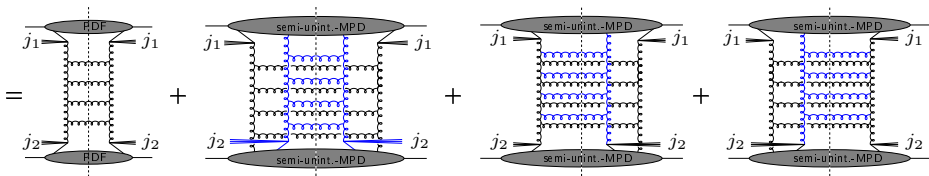
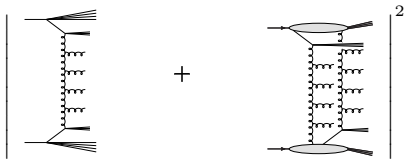


MN jets in MPI

here MPI = DPS (double parton scattering)



# Can Mueller-Navelet jets be a manifestation of multiparton interactions?



single  $\mathbb{P}$  ladder

two  $\mathbb{P}$  ladders

interferences

scaling:  $s^{\alpha_{\mathbb{P}}}$

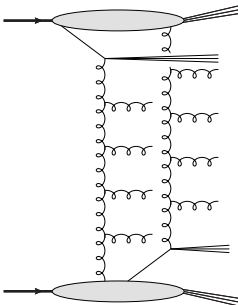
(??)  $s^{2\alpha_{\mathbb{P}}}$

??

- The twist counting is not easy for MPI kinds of contributions at small  $x$
- $k_{\perp 1,2}$  are not integrated  $\Rightarrow$  MPI may be competitive, and enhanced by small- $x$  resummation
- Interference terms are not governed by BJKP (this is not a fully interacting 3-reggeons system) (for BJKP,  $\alpha_{\mathbb{P}} < 1 \Rightarrow$  suppressed)

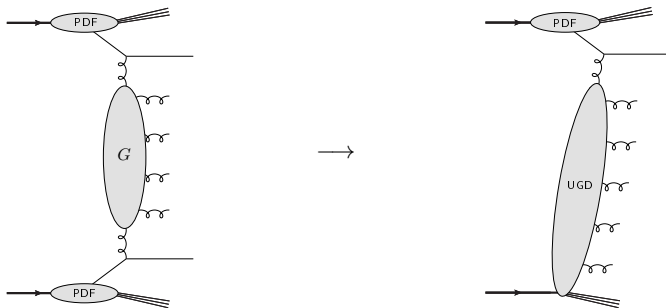
## A phenomenological test: the problem

- Simplification: we neglect any interference contribution between the two mechanisms
- How to evaluate the DPS contribution?



- This would require some kind of "hybrid" double parton distributions, with
  - one collinear parton
  - one off-shell parton (with some  $k_{\perp}$ )
- Almost nothing is known on such distributions

# A phenomenological test: our ansatz



Mueller-Navelet jets production at LL accuracy

Inclusive forward jet production

Factorized ansatz for the DPS contribution:

$$\sigma_{\text{DPS}} = \frac{\sigma_{\text{fwd}} \sigma_{\text{bwd}}}{\sigma_{\text{eff}}}$$

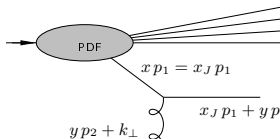
Tevatron, LHC:  $\sigma_{\text{eff}} \simeq 15 \text{ mb}$

To account for some discrepancy between various measurements, we take

$$\sigma_{\text{eff}} \simeq 10 - 20 \text{ mb}$$

# A phenomenological test: our ansatz

At LO for the jet vertex:



unintegrated gluon distribution (UGD):

$$\mathcal{F}_g \left( \frac{\mathbf{k}_J^2}{s x_J}, |\mathbf{k}_J| \right)$$

normalized according to:

$$\int d\mathbf{k}^2 \mathcal{F}_g(x, |\mathbf{k}|) = x f_g(x) \text{ (usual PDF)}$$

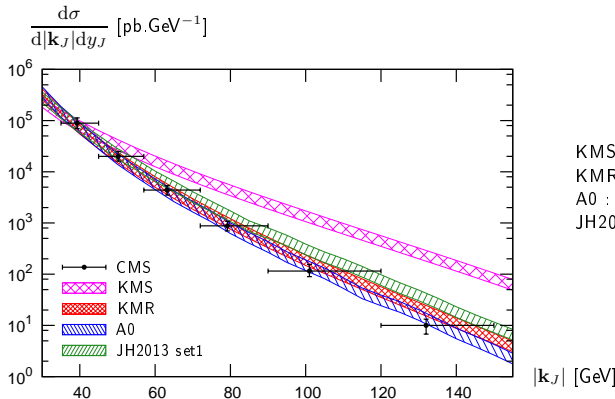
UGD

inclusive forward jet cross-section:

$$\frac{d\sigma}{d|\mathbf{k}_J| dy_J} = K \frac{\alpha_s}{|\mathbf{k}_J|} x_J (C_F f_q(x_J) + C_A f_g(x_J)) \mathcal{F}_g \left( \frac{\mathbf{k}_J^2}{s x_J}, |\mathbf{k}_J| \right)$$

## A phenomenological test

- We use CMS data at  $\sqrt{s} = 7$  TeV,  $3.2 < |y_J| < 4.7$
- We use various parametrization for the UGD
- For each parametrization we determine the range of  $K$  compatible with the CMS measurement in the lowest transverse momentum bin



	$K_{min}$	$K_{max}$
KMS :	1.20	1.94
KMR :	1.05	1.69
A0 :	4.27	6.89
JH2013 :	2.44	3.94

$$\frac{d\sigma}{d|\mathbf{k}_J|dy_J} = K \frac{\alpha_s}{|\mathbf{k}_J|} x_J (C_F f_q(x_J) + C_A f_g(x_J)) \mathcal{F}_g \left( \frac{\mathbf{k}_J^2}{s x_J}, |\mathbf{k}_J| \right)$$

# SPS vs DPS: Results

We will focus on four choices of kinematical cuts:

- $\sqrt{s} = 7$  TeV,  $|\mathbf{k}_{J1}| = |\mathbf{k}_{J2}| = 35$  GeV,  
(like in the CMS analysis for azimuthal correlations of MN jets)
- $\sqrt{s} = 14$  TeV,  $|\mathbf{k}_{J1}| = |\mathbf{k}_{J2}| = 35$  GeV,
- $\sqrt{s} = 14$  TeV,  $|\mathbf{k}_{J1}| = |\mathbf{k}_{J2}| = 20$  GeV,
- $\sqrt{s} = 14$  TeV,  $|\mathbf{k}_{J1}| = |\mathbf{k}_{J2}| = 10$  GeV ← highest DPS effect expected

parameters:

- $0 < y_{J,1} < 4.7$  and  $-4.7 < y_{J,2} < 0$
- MSTW 2008 parametrization for PDFs
- In the case of the NLL NFKL calculation, anti- $k_t$  jet algorithm with  $R = 0.5$ .

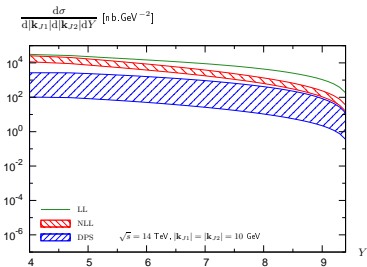
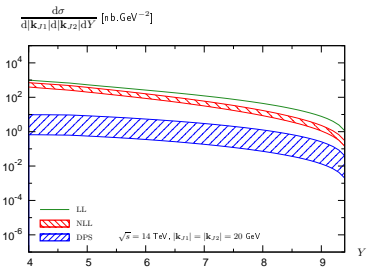
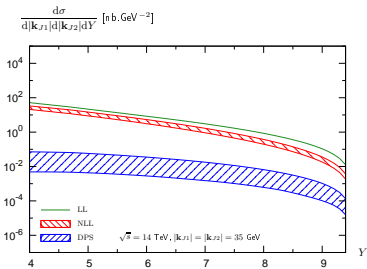
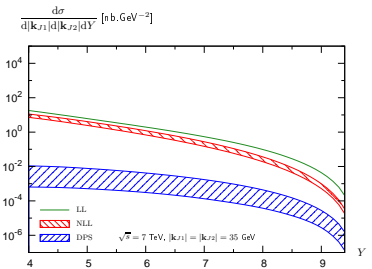
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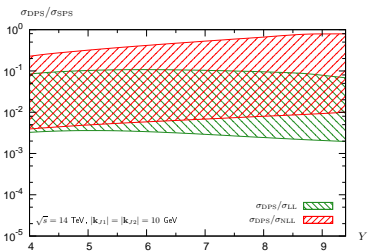
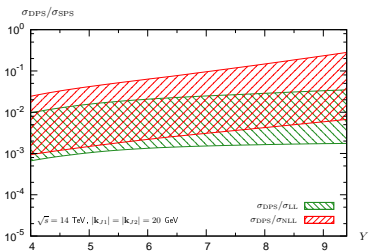
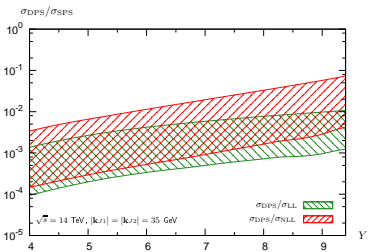
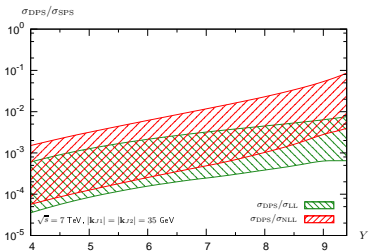
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## SPS vs DPS: cross-sections

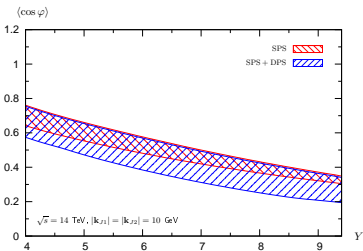
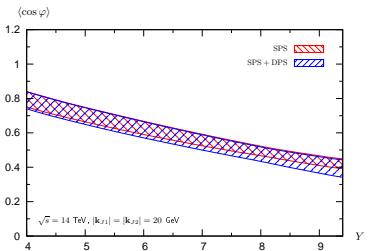
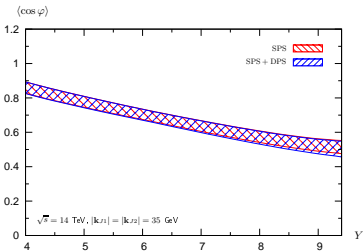
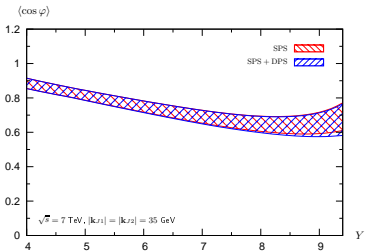


# SPS vs DPS: cross-sections (ratios)

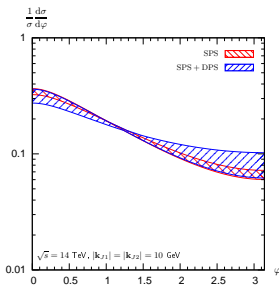
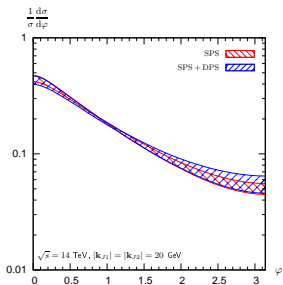
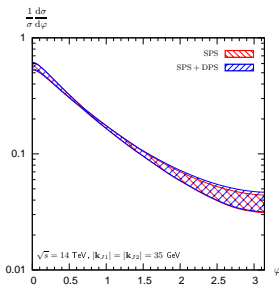
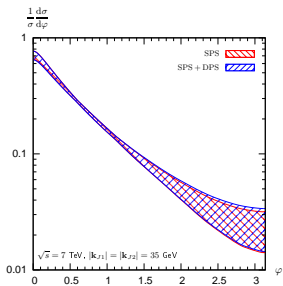




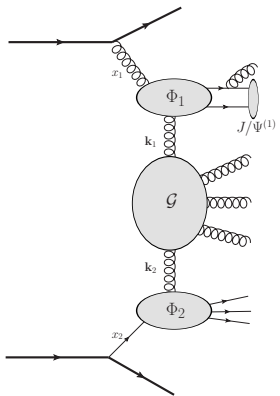
## SPS vs DPS: Azimuthal correlations



## SPS vs DPS: Azimuthal distributions

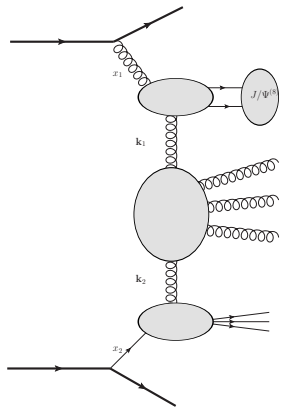
 $8 < Y < 9.4$

# Inclusive production of a forward $J/\psi$ + a backward jet



Color singlet mechanism

- Hard scales:  $k_J$  and  $M_{J/\psi}$
- Very promising at **ATLAS** (and **CMS**?)
- To be studied: cross-section study and azimuthal correlation



Color octet mechanism

Work in progress with LO vertex + NLO BFKL Green function

R. Boussarie, B. Ducloué, L. Szymanowski, S. W.

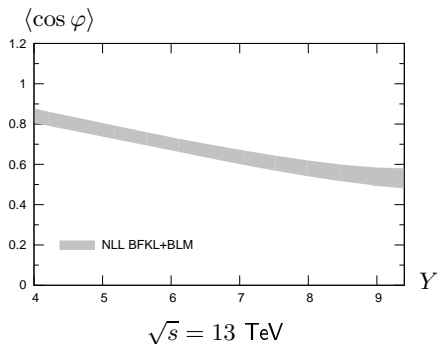
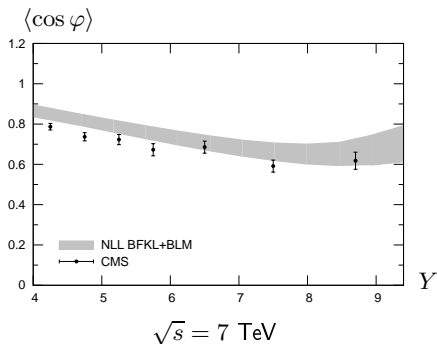
## Conclusions

- We studied **Mueller-Navelet** jets at full (vertex + Green's function) **NLL BFKL** accuracy and compared our results with the first data from the **LHC**
- The agreement with **CMS** data at 7 TeV is greatly improved by using the **BLM** scale fixing procedure
- $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$  is almost not affected by **BLM** and shows a clear difference between **NLO fixed-order** and **NLL BFKL** in an **asymmetric configuration**
- **Energy-momentum conservation** seems to be less severely violated with the NLO jet vertex
- We did the same analysis at 13 TeV: [see backup slides]
  - Azimuthal decorrelations at 13 TeV vs 7 TeV are similar
  - **NLL BFKL** predicts a stronger rise of the cross section with increasing energy than a **NLO fixed-order** calculation

**Measurement of the cross section at  $\sqrt{s} = 7$  or 8 TeV ?**
- We studied the effect of DPS contributions which could mimic the MN jet
  - For **cross-sections**: The uncertainty on DPS is very large. Still,  $\sigma_{DPS} < \sigma_{SPS}$  in the **LHC** kinematics
  - For **angular correlations**: including DPS **does not significantly modify our NLL BFKL prediction**
  - For low  $k_J$  and large  $Y$ , **the effect of DPS can become larger than the uncertainty on the NLL BFKL calculation.**  
One should focus on this region experimentally.

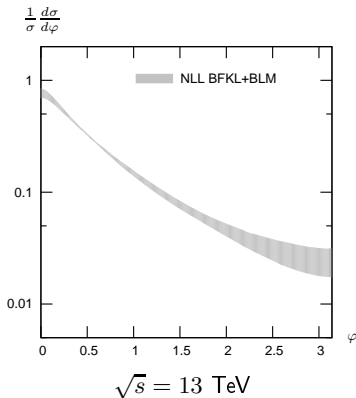
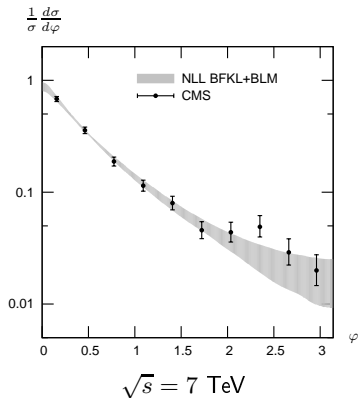
# Backup

## Azimuthal correlation $\langle \cos \varphi \rangle$



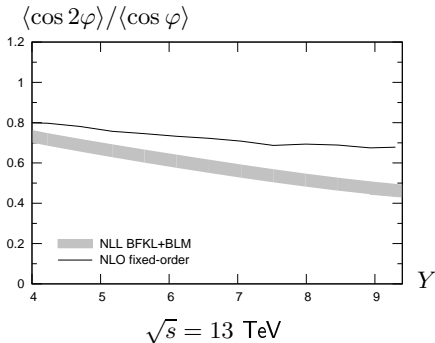
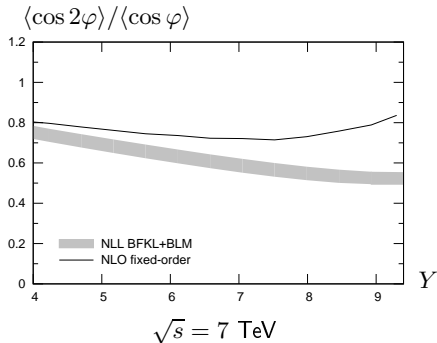
The behavior is similar at 13 TeV and at 7 TeV

Azimuthal distribution (integrated over  $6 < Y < 9.4$ )



The behavior is similar at 13 TeV and at 7 TeV

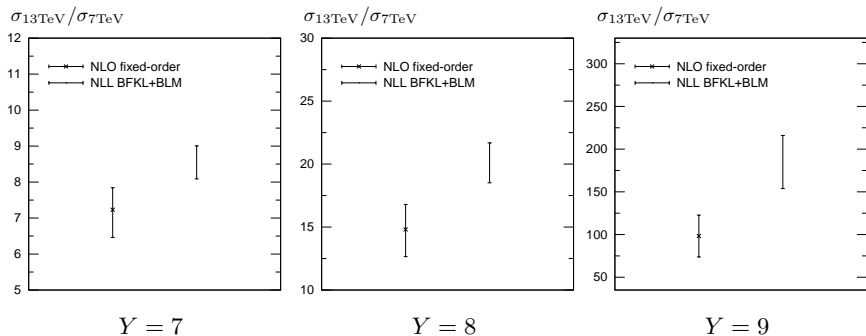
## Azimuthal correlation $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$ (asymmetric configuration)



The difference between BFKL and fixed-order is smaller at 13 TeV than at 7 TeV



## Cross section



It is useful to define the coefficients  $C_n$  as

$$C_n \equiv \int d\phi_{J1} d\phi_{J2} \cos(n(\phi_{J1} - \phi_{J2} - \pi)) \\ \times \int d^2\mathbf{k}_1 d^2\mathbf{k}_2 \Phi(\mathbf{k}_{J1}, x_{J1}, -\mathbf{k}_1) G(\mathbf{k}_1, \mathbf{k}_2, \hat{s}) \Phi(\mathbf{k}_{J2}, x_{J2}, \mathbf{k}_2)$$

- $n = 0 \implies$  differential cross-section

$$C_0 = \frac{d\sigma}{d|\mathbf{k}_{J1}| d|\mathbf{k}_{J2}| dy_{J1} dy_{J2}}$$

- $n > 0 \implies$  azimuthal decorrelation

$$\frac{C_n}{C_0} = \langle \cos(n(\phi_{J,1} - \phi_{J,2} - \pi)) \rangle \equiv \langle \cos(n\varphi) \rangle$$

- sum over  $n \implies$  azimuthal distribution

$$\frac{1}{\sigma} \frac{d\sigma}{d\varphi} = \frac{1}{2\pi} \left\{ 1 + 2 \sum_{n=1}^{\infty} \cos(n\varphi) \langle \cos(n\varphi) \rangle \right\}$$