

Mueller-Navelet Jets at the LHC: Evidence for High-Energy Resummation Effects

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in collaboration with

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D. Colferai, F. Schwennsen, L. Szymanowski, S. W., JHEP 1012 (2010) 026 [arXiv:1002.1365 [hep-ph]]

B. Ducloué, L. Szymanowski, S. W., JHEP 1305 (2013) 096 [arXiv:1302.7012 [hep-ph]]

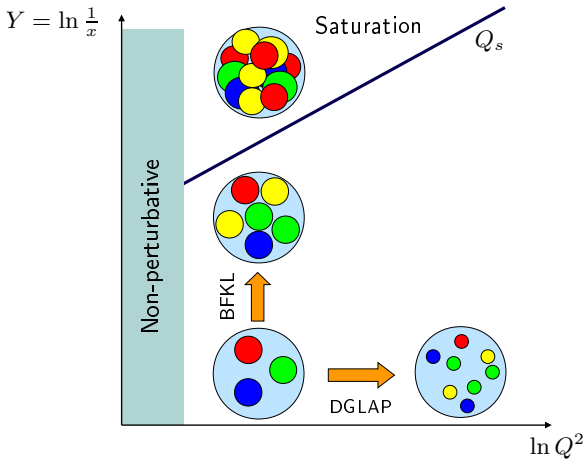
B. Ducloué, L. Szymanowski, S. W., Phys. Rev. Lett. 112 (2014) 082003 [arXiv:1309.3229 [hep-ph]]

B. Ducloué, L. Szymanowski, S. W., Phys. Lett. B738 (2014) 311-316 [arXiv:1407.6593 [hep-ph]]

B. Ducloué, L. Szymanowski, S. W., *to be submitted*

R. Boussarie, B. Ducloué, L. Szymanowski, S. W., *in preparation*

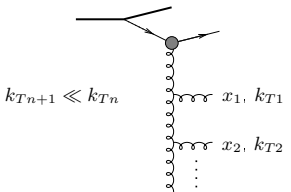
The different regimes of QCD



Resummation in QCD: DGLAP vs BFKL

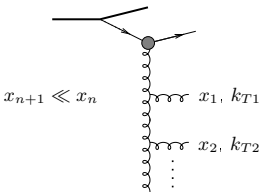
Small values of α_s (perturbation theory applies if there is a hard scale) can be compensated by large logarithmic enhancements.

DGLAP

strong ordering in k_T

$$\sum (\alpha_s \ln Q^2)^n$$

BFKL

strong ordering in x

$$\sum (\alpha_s \ln s)^n$$

When \sqrt{s} becomes very large, it is expected that a BFKL description is needed to get accurate predictions

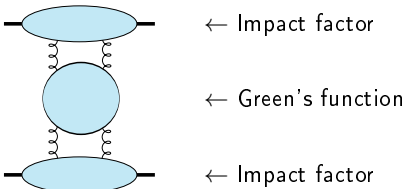
The specific case of QCD at large s

QCD in the perturbative Regge limit

The amplitude can be written as:

$$\mathcal{A} = \underbrace{\text{Diagram 1}}_{\sim s} + \left(\underbrace{\text{Diagram 2}}_{\sim s (\alpha_s \ln s)} + \underbrace{\text{Diagram 3}}_{\sim s (\alpha_s \ln s)} + \dots \right) + \left(\underbrace{\text{Diagram 4}}_{\sim s (\alpha_s \ln s)^2} + \dots \right) + \dots$$

this can be put in the following form :



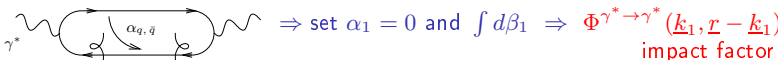
$$\sigma_{tot}^{h_1 h_2 \rightarrow \text{anything}} = \frac{1}{s} \text{Im} \mathcal{A} \sim s^{\alpha_{\mathbb{P}}(0) - 1}$$

with $\alpha_{\mathbb{P}}(0) - 1 = C \alpha_s + C' \alpha_s^2 + \dots$

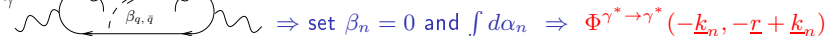
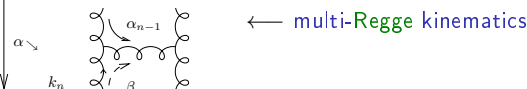
$C > 0$: Leading Log \mathbb{P} omeron
Balitsky, Fadin, Kuraev, Lipatov

Opening the boxes: Impact representation $\gamma^* \gamma^* \rightarrow \gamma^* \gamma^*$ as an example

- **Sudakov** decomposition: $k_i = \alpha_i p_1 + \beta_i p_2 + k_{\perp i}$ ($p_1^2 = p_2^2 = 0$, $2p_1 \cdot p_2 = s$)
- write $d^4 k_i = \frac{s}{2} d\alpha_i d\beta_i d^2 k_{\perp i}$ ($\underline{k} = \text{Eucl.} \leftrightarrow k_{\perp} = \text{Mink.}$)
- t -channel gluons have **non-sense** polarizations at large s : $\epsilon_{NS}^{up/down} = \frac{2}{s} p_{2/1}$



$$\mathcal{M} = \frac{is}{(2\pi)^2} \int \frac{d^2 \underline{k}}{\underline{k}^2} \Phi^{up}(\underline{k}, \underline{r} - \underline{k}) \int \frac{d^2 \underline{k}'}{\underline{k}'^2} \Phi^{down}(-\underline{k}', -\underline{r} + \underline{k}') \\ \times \int_{\delta-i\infty}^{\delta+i\infty} \frac{d\omega}{2\pi i} \left(\frac{s}{s_0}\right)^\omega G_\omega(\underline{k}, \underline{k}', \underline{r})$$



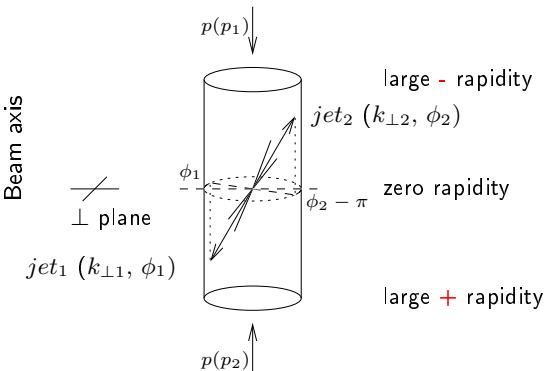
Higher order corrections

- Higher order corrections to BFKL kernel are known at NLL order (Lipatov Fadin; Camici, Ciafaloni), now for arbitrary impact parameter $\alpha_S \sum_n (\alpha_S \ln s)^n$ resummation
- impact factors are known in some cases at NLL
 - $\gamma^* \rightarrow \gamma^*$ at $t = 0$ (Bartels, Colferai, Gieseke, Kyrieleis, Qiao; Balitski, Chirilli)
 - forward jet production (Bartels, Colferai, Vacca; Caporale, Ivanov, Murdaca, Papa, Perri; Chachamis, Hentschinski, Madrigal, Sabio Vera)
 - inclusive production of a pair of hadrons separated by a large interval of rapidity (Ivanov, Papa)
 - $\gamma_L^* \rightarrow \rho_L$ in the forward limit (Ivanov, Kotsky, Papa)

Mueller-Navelet jets: Basics

Mueller-Navelet jets

- Consider two jets (hadrons flying within a narrow cone) **separated by a large rapidity**, i.e. each of them almost fly in the direction of the hadron “close” to it, and with very similar transverse momenta
- Pure LO *collinear* treatment: these two jets should be emitted **back to back** at leading order: $\Delta\phi - \pi = 0$ ($\Delta\phi = \phi_1 - \phi_2 =$ relative azimuthal angle) and $k_{\perp 1} = k_{\perp 2}$. No phase space for (untagged) emission between them



Master formulas

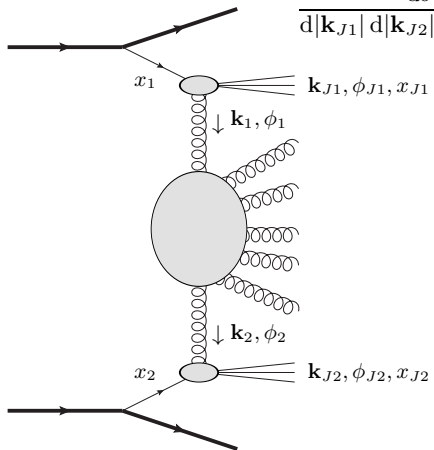
 k_T -factorized differential cross section

$$\frac{d\sigma}{d|\mathbf{k}_{J1}| d|\mathbf{k}_{J2}| dy_{J1} dy_{J2}} = \int d\phi_{J1} d\phi_{J2} \int d^2\mathbf{k}_1 d^2\mathbf{k}_2$$

$$\times \Phi(\mathbf{k}_{J1}, x_{J1}, -\mathbf{k}_1)$$

$$\times G(\mathbf{k}_1, \mathbf{k}_2, \hat{s})$$

$$\times \Phi(\mathbf{k}_{J2}, x_{J2}, \mathbf{k}_2)$$



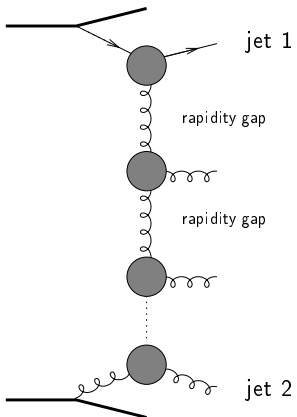
$$\text{with } \Phi(\mathbf{k}_{J2}, x_{J2}, \mathbf{k}_2) = \int dx_2 f(x_2) V(\mathbf{k}_2, x_2)$$

$$f \equiv \text{PDF}$$

$$x_J = \frac{|\mathbf{k}_J|}{\sqrt{s}} e^{y_J}$$

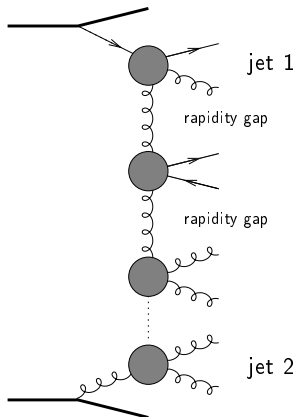
Mueller-Navelet jets: LL vs NLL

LL BFKL



$$\sum (\alpha_s \ln s)^n$$

NLL BFKL



$$\sum (\alpha_s \ln s)^n + \alpha_s \sum (\alpha_s \ln s)^n$$

Results

Results for a symmetric configuration

In the following we show results for

- $\sqrt{s} = 7 \text{ TeV}$
- $35 \text{ GeV} < |\mathbf{k}_{J1}|, |\mathbf{k}_{J2}| < 60 \text{ GeV}$
- $0 < |y_1|, |y_2| < 4.7$

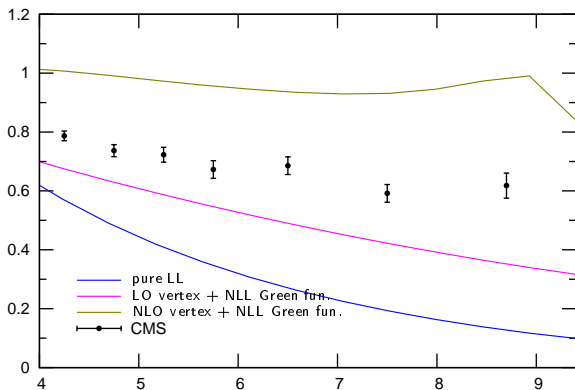
These cuts allow us to compare our predictions with the first experimental data on azimuthal correlations of [Mueller-Navelet](#) jets at the LHC presented by the [CMS](#) collaboration (CMS-PAS-FSQ-12-002)

note: unlike experiments we have to set an upper cut on $|\mathbf{k}_{J1}|$ and $|\mathbf{k}_{J2}|$. We have checked that our results do not depend on this cut significantly.

Results: azimuthal correlations

Azimuthal correlation $\langle \cos \varphi \rangle$

$$\frac{c_1}{c_0} = \langle \cos \varphi \rangle \equiv \langle \cos(\phi_{J1} - \phi_{J2} - \pi) \rangle$$


 $35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$
 $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$
 $0 < |y_1| < 4.7$
 $0 < |y_2| < 4.7$
 $Y \equiv |y_1 - y_2|$

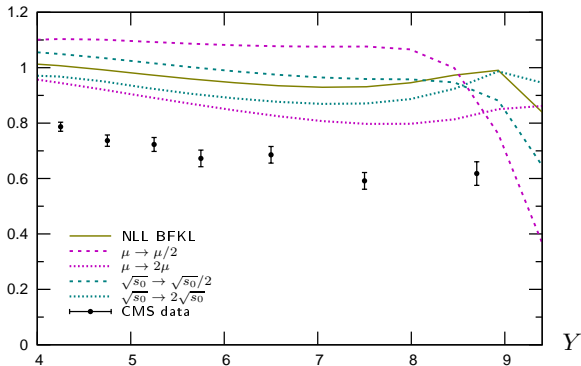
The NLO corrections to the jet vertex lead to a large increase of the correlation

Note: LO vertex + NLL Green done by F. Schwennsen, A. Sabio-Vera; C. Marquet, C. Royon

Results: azimuthal correlations

Azimuthal correlation $\langle \cos \varphi \rangle$

$$\langle \cos \varphi \rangle \equiv \langle \cos(\phi_{J1} - \phi_{J2} - \pi) \rangle$$



$$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$$

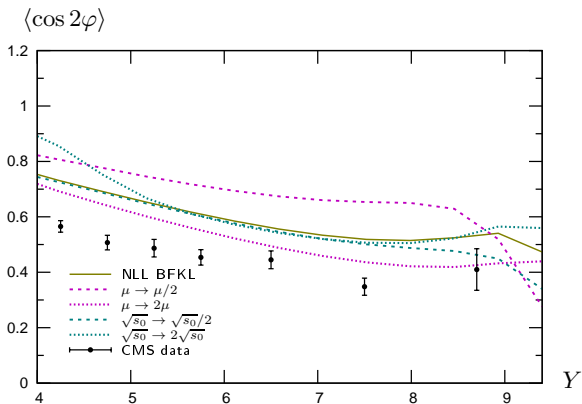
$$35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$$

$$0 < |y_1| < 4.7$$

$$0 < |y_2| < 4.7$$

- NLL BFKL predicts a too small decorrelation
- The NLL BFKL calculation is still rather dependent on the scales, especially the renormalization / factorization scale

Results: azimuthal correlations

Azimuthal correlation $\langle \cos 2\varphi \rangle$ 

$$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$$

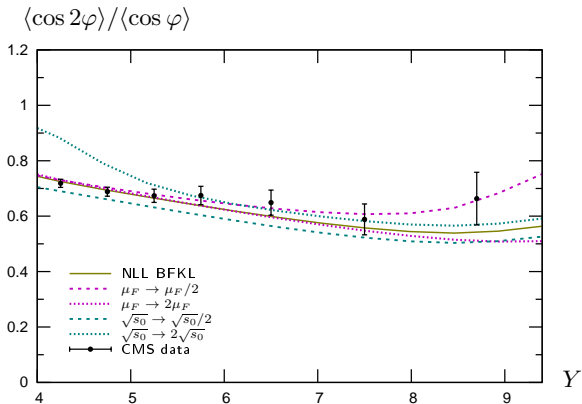
$$35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$$

$$0 < |y_1| < 4.7$$

$$0 < |y_2| < 4.7$$

- The agreement with data is a little better for $\langle \cos 2\varphi \rangle$ but still not very good
- This observable is also very sensitive to the scales

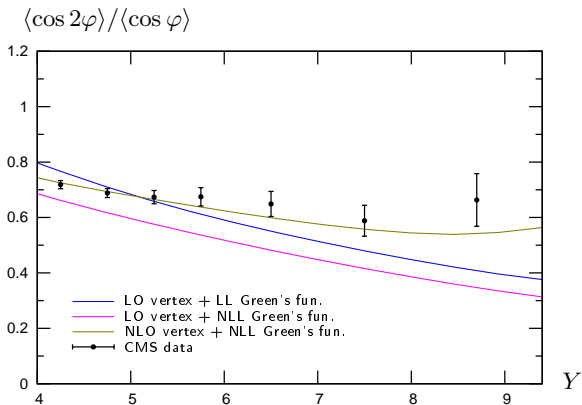
Results: azimuthal correlations

Azimuthal correlation $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$  $35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$ $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$ $0 < |y_1| < 4.7$ $0 < |y_2| < 4.7$

- This observable is more stable with respect to the scales than the previous ones
- The agreement with data is good across the whole Y range

Results: azimuthal correlations

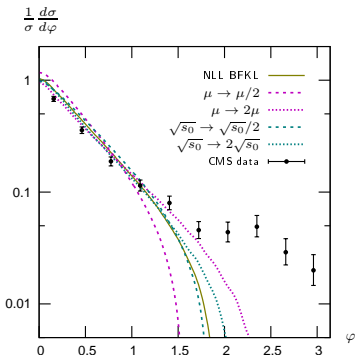
Azimuthal correlation $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$



$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$
 $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$
 $0 < |y_1| < 4.7$
 $0 < |y_2| < 4.7$

It is necessary to include the NLO corrections to the jet vertex to reproduce the behavior of the data at large Y

Results: azimuthal distribution

Azimuthal distribution (integrated over $6 < Y < 9.4$)

$$\frac{1}{\sigma} \frac{d\sigma}{d\varphi} = \frac{1}{2\pi} \left\{ 1 + 2 \sum_{n=1}^{\infty} \cos(n\varphi) \langle \cos(n\varphi) \rangle \right\}.$$

- Our calculation predicts a too large value of $\frac{1}{\sigma} \frac{d\sigma}{d\varphi}$ for $\varphi \lesssim \frac{\pi}{2}$ and a too small value for $\varphi \gtrsim \frac{\pi}{2}$
- It is not possible to describe the data even when varying the scales by a factor of 2

Results: limitations

- The agreement of our calculation with the data for $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$ is good and quite stable with respect to the scales
- The agreement for $\langle \cos n\varphi \rangle$ and $\frac{1}{\sigma} \frac{d\sigma}{d\varphi}$ is not very good and very sensitive to the choice of the renormalization scale μ_R
- An all-order calculation would be independent of the choice of μ_R . This feature is lost if we truncate the perturbative series
 - ⇒ How to choose the renormalization scale?
 - 'Natural scale': sometimes the typical momenta in a loop diagram are different from the natural scale of the process

We decided to use the **Brody-Lepage-Mackenzie (BLM)** procedure to fix the renormalization scale

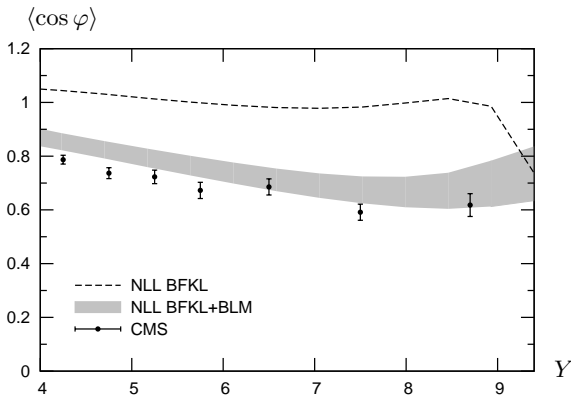
The BLM renormalization scale fixing procedure

The **Brodsky-Lepage-Mackenzie (BLM)** procedure resums the self-energy corrections to the gluon propagator at one loop into the running coupling.

First attempts to apply **BLM** scale fixing to **BFKL** processes lead to problematic results. **Brodsky, Fadin, Kim, Lipatov and Pivovarov** suggested that one should first go to a physical renormalization scheme like MOM and then apply the 'traditional' **BLM** procedure, i.e. identify the β_0 dependent part and choose μ_R such that it vanishes.

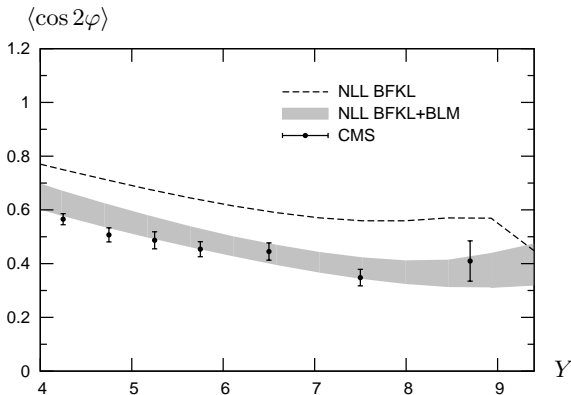
We followed this prescription for the full amplitude at NLL.

Results with BLM

Azimuthal correlation $\langle \cos \varphi \rangle$ 
 $35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$
 $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$
 $0 < |y_1| < 4.7$
 $0 < |y_2| < 4.7$

Using the BLM scale setting, the agreement with data becomes much better

Results with BLM

Azimuthal correlation $\langle \cos 2\varphi \rangle$ 

$$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$$

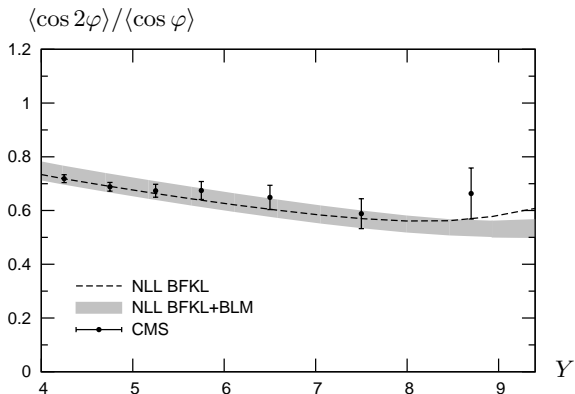
$$35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$$

$$0 < |y_1| < 4.7$$

$$0 < |y_2| < 4.7$$

Using the BLM scale setting, the agreement with data becomes much better.

Results with BLM

Azimuthal correlation $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$ 

$$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$$

$$35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$$

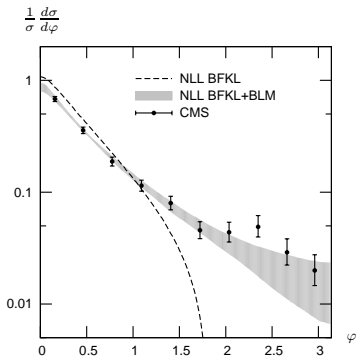
$$0 < |y_1| < 4.7$$

$$0 < |y_2| < 4.7$$

Because it is much less dependent on the scales, the observable $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$ is almost not affected by the BLM procedure and is still in good agreement with the data.

Results with BLM

Azimuthal distribution (integrated over $6 < Y < 9.4$)



With the BLM scale setting the azimuthal distribution is in good agreement with the data across the full φ range.

Comparison with fixed-order

Using the **BLM** scale setting:

- The agreement $\langle \cos n\varphi \rangle$ with the data becomes much better
- The agreement for $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$ is still good and unchanged as this observable is weakly dependent on μ_R
- The azimuthal distribution is in much better agreement with the data

But the configuration chosen by **CMS** with $\mathbf{k}_{J_{\min 1}} = \mathbf{k}_{J_{\min 2}}$ does not allow us to compare with a **fixed-order** $\mathcal{O}(\alpha_s^3)$ treatment (i.e. without resummation)

- These calculations are unstable when $\mathbf{k}_{J_{\min 1}} = \mathbf{k}_{J_{\min 2}}$ because the cancellation of some divergencies is difficult to obtain numerically
- Presumably, resummation effects à la **Sudakov** could be important in the limit $\mathbf{k}_{J_1} \simeq \mathbf{k}_{J_2}$ and require a special treatment

Comparison with fixed-order

Results for an asymmetric configuration

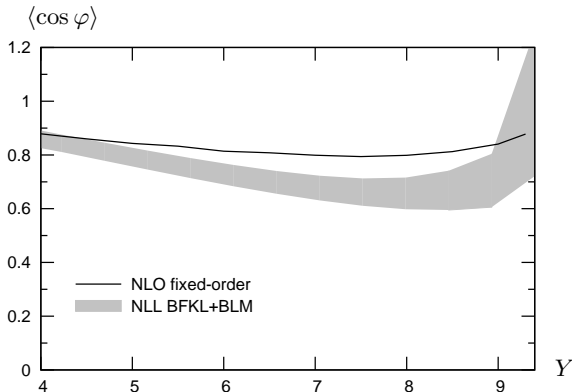
In this section we choose the cuts as

- $35 \text{ GeV} < |\mathbf{k}_{J1}|, |\mathbf{k}_{J2}| < 60 \text{ GeV}$
- $50 \text{ GeV} < \text{Max}(|\mathbf{k}_{J1}|, |\mathbf{k}_{J2}|)$
- $0 < |y_1|, |y_2| < 4.7$

and we compare our results with the NLO fixed-order code Dijet ([Aurenche, Basu, Fontannaz](#)) in the same configuration

Comparison with fixed-order

Azimuthal correlation $\langle \cos \varphi \rangle$

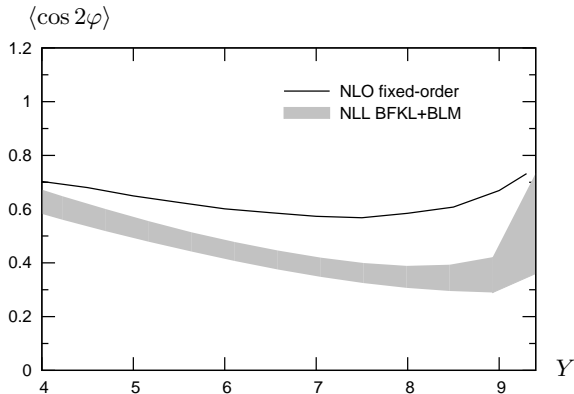


$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$
 $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$
 $50 \text{ GeV} < \text{Max}(|\mathbf{k}_{J1}|, |\mathbf{k}_{J2}|)$
 $0 < |y_1| < 4.7$
 $0 < |y_2| < 4.7$

The NLO fixed-order and NLL BFKL+BLM calculations are very close

Comparison with fixed-order

Azimuthal correlation $\langle \cos 2\varphi \rangle$



$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$

$35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$

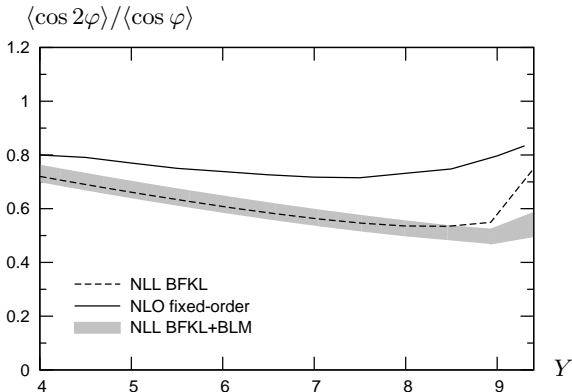
$50 \text{ GeV} < \text{Max}(|\mathbf{k}_{J1}|, |\mathbf{k}_{J2}|)$

$0 < |y_1| < 4.7$

$0 < |y_2| < 4.7$

The **BLM** procedure leads to a **sizable difference** between **NLO fixed-order** and **NLL BFKL+BLM**.

Comparison with fixed-order

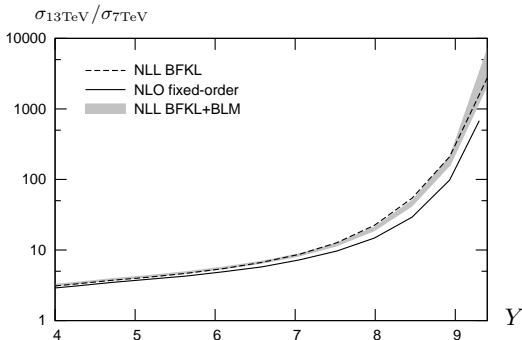
Azimuthal correlation $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$ 

$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$
 $35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$
 $50 \text{ GeV} < \text{Max}(|\mathbf{k}_{J1}|, |\mathbf{k}_{J2}|)$
 $0 < |y_1| < 4.7$
 $0 < |y_2| < 4.7$

Using **BLM** or not, there is a **sizable difference** between **BFKL** and fixed-order.

Comparison with fixed-order

Cross section: 13 TeV vs. 7 TeV



$35 \text{ GeV} < |\mathbf{k}_{J1}| < 60 \text{ GeV}$

$35 \text{ GeV} < |\mathbf{k}_{J2}| < 60 \text{ GeV}$

$50 \text{ GeV} < \text{Max}(|\mathbf{k}_{J1}|, |\mathbf{k}_{J2}|)$

$0 < |y_1| < 4.7$

$0 < |y_2| < 4.7$

- In a **BFKL** treatment, a **strong rise of the cross section with increasing energy** is expected.
- This rise is faster than in a fixed-order treatment

Energy-momentum conservation

- It is necessary to have $\mathbf{k}_{J_{\min 1}} \neq \mathbf{k}_{J_{\min 2}}$ for comparison with fixed order calculations but this can be problematic for **BFKL** because of energy-momentum conservation
- There is no strict energy-momentum conservation in **BFKL**
- This was studied at LO by **Del Duca and Schmidt**. They introduced an effective rapidity Y_{eff} defined as

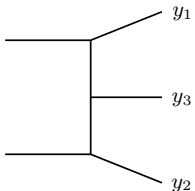
$$Y_{\text{eff}} \equiv Y \frac{\sigma^{2 \rightarrow 3}}{\sigma^{\text{BFKL}, \mathcal{O}(\alpha_s^3)}}$$

- When one replaces Y by Y_{eff} in the expression of σ^{BFKL} and truncates to $\mathcal{O}(\alpha_s^3)$, the exact $2 \rightarrow 3$ result is obtained

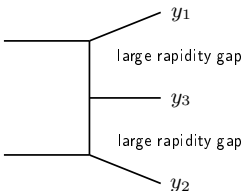
Energy-momentum conservation

We follow the idea of [Del Duca and Schmidt](#), adding the NLO jet vertex contribution:

exact $2 \rightarrow 3$

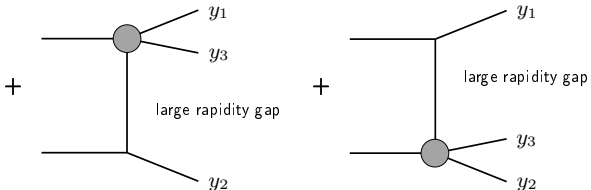


BFKL



one emission from the Green's function + LO jet vertex

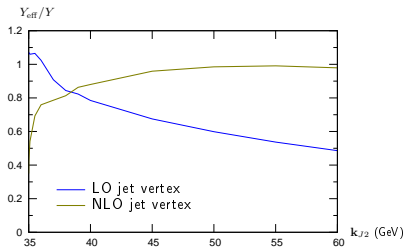
we have to take into account these additional $\mathcal{O}(\alpha_s^3)$ contributions:



no emission from the Green's function + NLO jet vertex

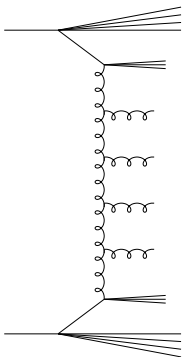
Energy-momentum conservation

Variation of Y_{eff}/Y as a function of k_{J2} for fixed $k_{J1} = 35$ GeV (with $\sqrt{s} = 7$ TeV, $Y = 8$):



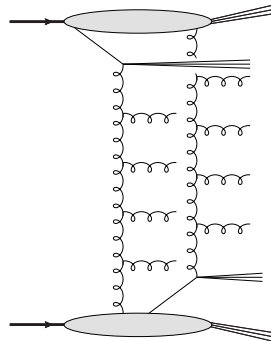
- With the **LO** jet vertex, Y_{eff} is much smaller than Y when k_{J1} and k_{J2} are significantly different
- This is the region important for comparison with fixed order calculations
- The improvement coming from the **NLO** jet vertex is very large in this region
- For $k_{J1} = 35$ GeV and $k_{J2} = 50$ GeV, typical of the values we used for comparison with fixed order, we get $\frac{Y_{\text{eff}}}{Y} \simeq 0.98$ at NLO vs. ~ 0.6 at LO

Can Mueller-Navelet jets be a manifestation of multiparton interactions?



MN jets in the single partonic model

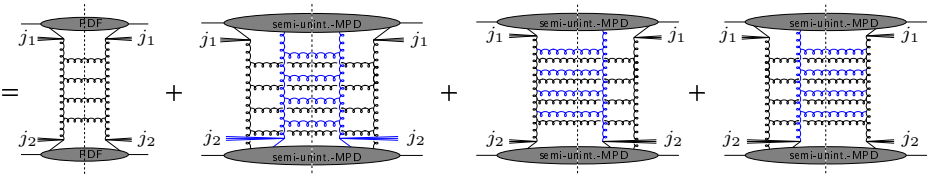
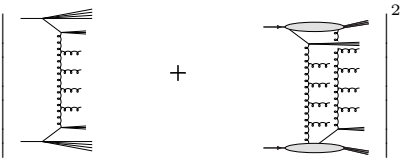
+



MN jets in MPI

here MPI = DPS (double parton scattering)

Can Mueller-Navelet jets be a manifestation of multiparton interactions?



single \mathbb{P} ladder

two \mathbb{P} ladders

interferences

scaling: $s^{\alpha_{\mathbb{P}}}$

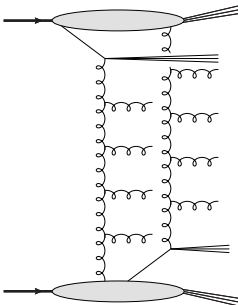
(??) $s^{2\alpha_{\mathbb{P}}}$

??

- The twist counting is not easy for MPI kinds of contributions at small x
- $k_{\perp 1,2}$ are not integrated \Rightarrow MPI may be competitive, and enhanced by small- x resummation
- Interference terms are not governed by BJKP (this is not a fully interacting 3-reggeons system) (for BJKP, $\alpha_{\mathbb{P}} < 1 \Rightarrow$ suppressed)

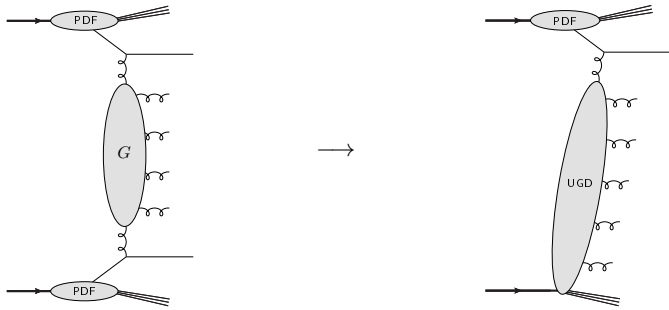
A phenomenological test: the problem

- Simplification: we neglect any interference contribution between the two mechanisms
- How to evaluate the DPS contribution?



- This would require some kind of "hybrid" double parton distributions, with
 - one collinear parton
 - one off-shell parton (with some k_{\perp})
- Almost nothing is known on such distributions

A phenomenological test: our ansatz



Mueller-Navelet jets production at LL accuracy

Inclusive forward jet production

Factorized ansatz for the DPS contribution:

$$\sigma_{\text{DPS}} = \frac{\sigma_{\text{fwd}} \sigma_{\text{bwd}}}{\sigma_{\text{eff}}}$$

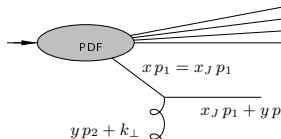
Tevatron, LHC: $\sigma_{\text{eff}} \simeq 15 \text{ mb}$

To account for some discrepancy between various measurements, we take

$$\sigma_{\text{eff}} \simeq 10 - 20 \text{ mb}$$

A phenomenological test: our ansatz

At LO for the jet vertex:



($y = \frac{\mathbf{k}_J^2}{s x_J}$: on-shell cond.)

unintegrated gluon distribution (UGD):

$$\mathcal{F}_g \left(\frac{\mathbf{k}_J^2}{s x_J}, |\mathbf{k}_J| \right)$$

normalized according to:

$$\int d\mathbf{k}^2 \mathcal{F}_g(x, |\mathbf{k}|) = x f_g(x) \text{ (usual PDF)}$$

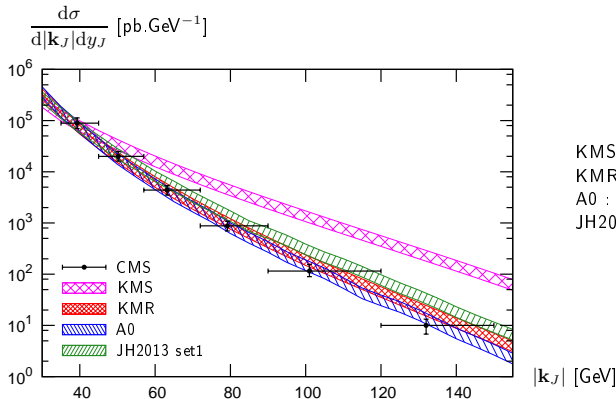
UGD

inclusive forward jet cross-section:

$$\frac{d\sigma}{d|\mathbf{k}_J| dy_J} = K \frac{\alpha_s}{|\mathbf{k}_J|} x_J (C_F f_q(x_J) + C_A f_g(x_J)) \mathcal{F}_g \left(\frac{\mathbf{k}_J^2}{s x_J}, |\mathbf{k}_J| \right)$$

A phenomenological test

- We use CMS data at $\sqrt{s} = 7$ TeV, $3.2 < |y_J| < 4.7$
- We use various parametrization for the UGD
- For each parametrization we determine the range of K compatible with the CMS measurement in the lowest transverse momentum bin



| | K_{min} | K_{max} |
|----------|-----------|-----------|
| KMS : | 1.20 | 1.94 |
| KMR : | 1.05 | 1.69 |
| A0 : | 4.27 | 6.89 |
| JH2013 : | 2.44 | 3.94 |

$$\frac{d\sigma}{d|\mathbf{k}_J|dy_J} = K \frac{\alpha_s}{|\mathbf{k}_J|} x_J (C_F f_q(x_J) + C_A f_g(x_J)) \mathcal{F}_g \left(\frac{\mathbf{k}_J^2}{s x_J}, |\mathbf{k}_J| \right)$$

SPS vs DPS: Results

We will focus on four choices of kinematical cuts:

- $\sqrt{s} = 7$ TeV, $|\mathbf{k}_{J1}| = |\mathbf{k}_{J2}| = 35$ GeV,
(like in the CMS analysis for azimuthal correlations of MN jets)
- $\sqrt{s} = 14$ TeV, $|\mathbf{k}_{J1}| = |\mathbf{k}_{J2}| = 35$ GeV,
- $\sqrt{s} = 14$ TeV, $|\mathbf{k}_{J1}| = |\mathbf{k}_{J2}| = 20$ GeV,
- $\sqrt{s} = 14$ TeV, $|\mathbf{k}_{J1}| = |\mathbf{k}_{J2}| = 10$ GeV ← highest DPS effect expected

parameters:

- $0 < y_{J,1} < 4.7$ and $-4.7 < y_{J,2} < 0$
- MSTW 2008 parametrization for PDFs
- In the case of the NLL NFKL calculation, anti- k_t jet algorithm with $R = 0.5$.

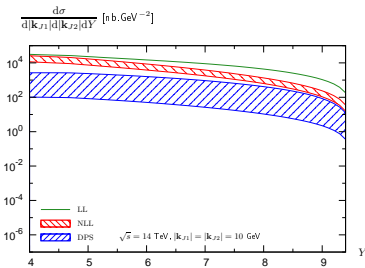
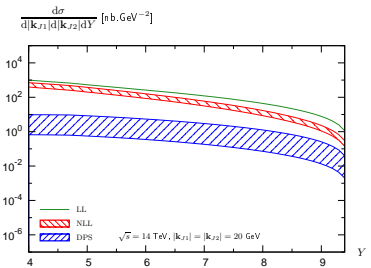
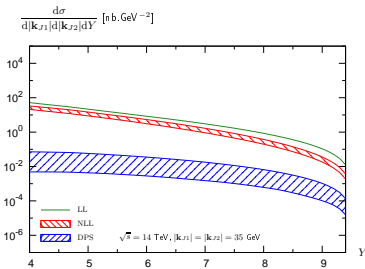
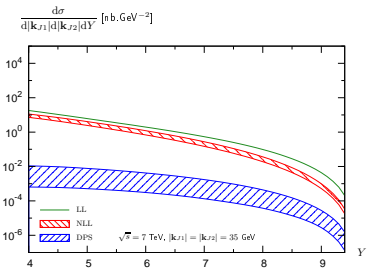
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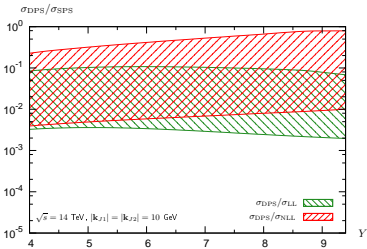
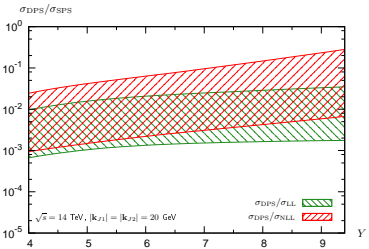
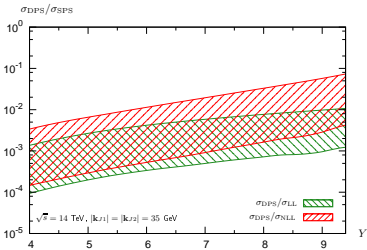
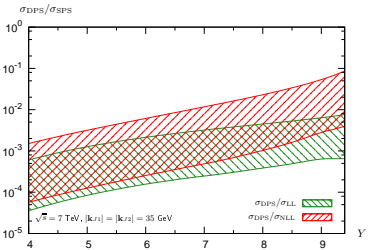
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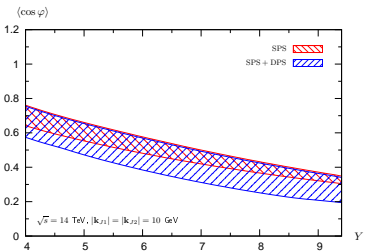
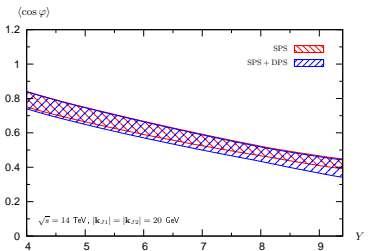
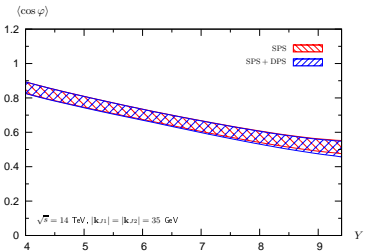
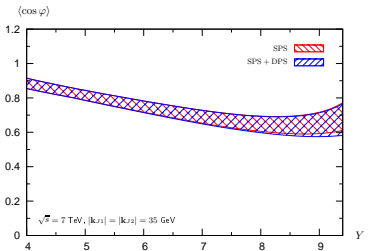
SPS vs DPS: cross-sections



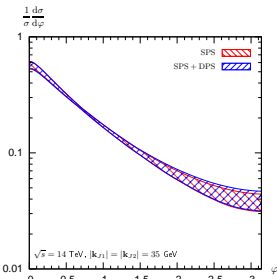
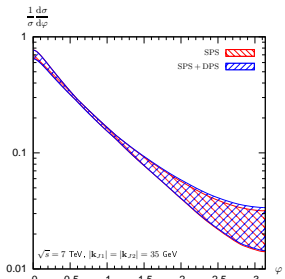
SPS vs DPS: cross-sections (ratios)



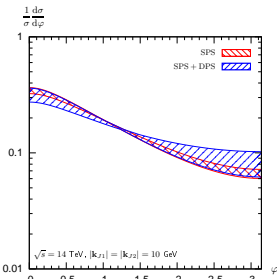
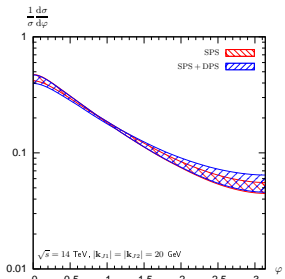
SPS vs DPS: Azimuthal correlations



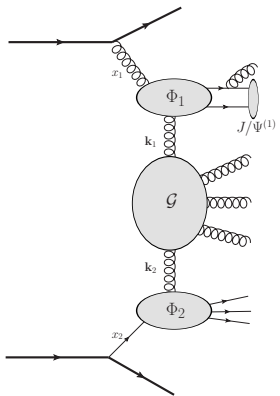
SPS vs DPS: Azimuthal distributions



$8 < Y < 9.4$

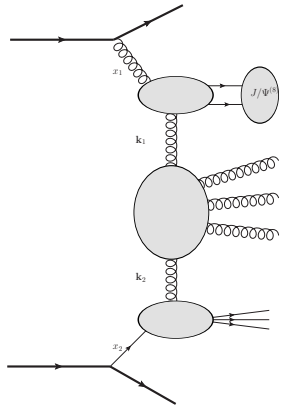


Inclusive production of a forward J/ψ + a backward jet



Color singlet mechanism

- Hard scales: k_J and $M_{J/\psi}$
- Very promising at **ATLAS** (and **CMS**?)
- To be studied: cross-section study and azimuthal correlation



Color octet mechanism

Work in progress with LO vertex + NLO BFKL Green function
R. Boussarie, B. Ducloué, L. Szymanowski, S. W.

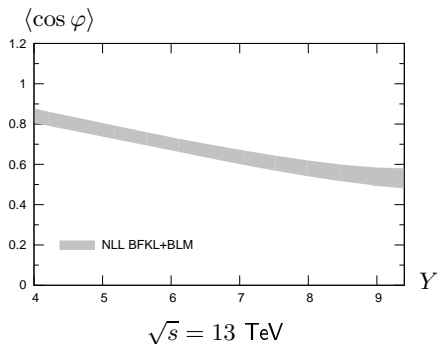
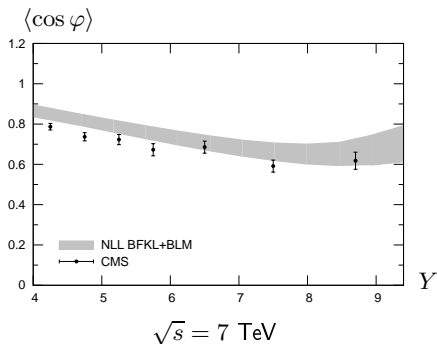
Conclusions

- We studied **Mueller-Navelet** jets at full (vertex + Green's function) **NLL BFKL** accuracy and compared our results with the first data from the **LHC**
- The agreement with **CMS** data at 7 TeV is greatly improved by using the **BLM** scale fixing procedure
- $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$ is almost not affected by **BLM** and shows a clear difference between **NLO fixed-order** and **NLL BFKL** in an **asymmetric configuration**
- **Energy-momentum conservation** seems to be less severely violated with the NLO jet vertex
- We did the same analysis at 13 TeV: [see backup slides]
 - Azimuthal decorrelations at 13 TeV vs 7 TeV are similar
 - **NLL BFKL** predicts a stronger rise of the cross section with increasing energy than a **NLO fixed-order** calculation

Measurement of the cross section at $\sqrt{s} = 7$ or 8 TeV ?
- We studied the effect of DPS contributions which could mimic the MN jet
 - For **cross-sections**: The uncertainty on DPS is very large. Still, $\sigma_{DPS} < \sigma_{SPS}$ in the **LHC** kinematics
 - For **angular correlations**: including DPS **does not significantly modify our NLL BFKL prediction**
 - For low k_J and large Y , the effect of DPS can become larger than the uncertainty on the **NLL BFKL** calculation. One should focus on this region experimentally.

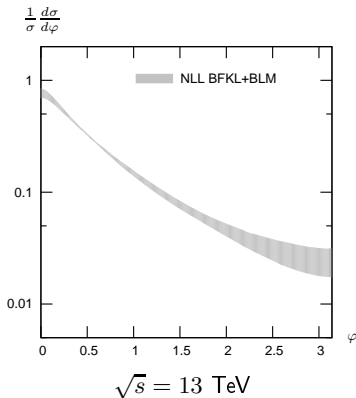
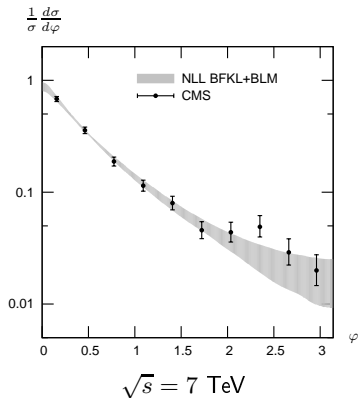
Backup

Azimuthal correlation $\langle \cos \varphi \rangle$



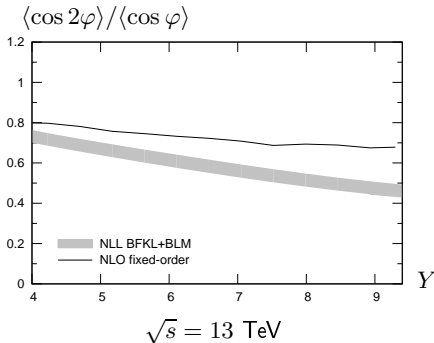
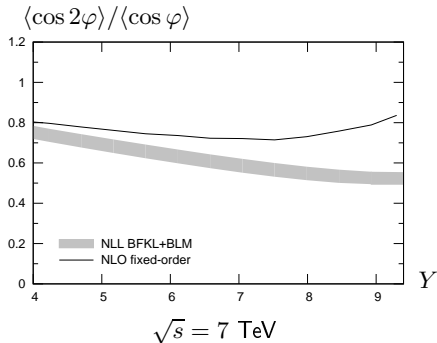
The behavior is similar at 13 TeV and at 7 TeV

Azimuthal distribution (integrated over $6 < Y < 9.4$)



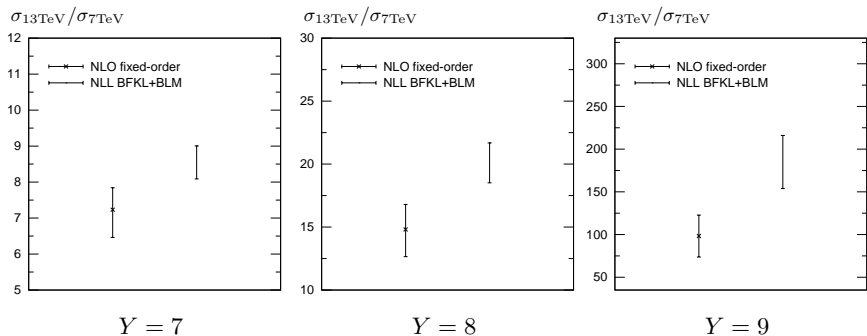
The behavior is similar at 13 TeV and at 7 TeV

Azimuthal correlation $\langle \cos 2\varphi \rangle / \langle \cos \varphi \rangle$ (asymmetric configuration)



The difference between BFKL and fixed-order is smaller at 13 TeV than at 7 TeV

Cross section



It is useful to define the coefficients C_n as

$$C_n \equiv \int d\phi_{J1} d\phi_{J2} \cos(n(\phi_{J1} - \phi_{J2} - \pi)) \\ \times \int d^2\mathbf{k}_1 d^2\mathbf{k}_2 \Phi(\mathbf{k}_{J1}, x_{J1}, -\mathbf{k}_1) G(\mathbf{k}_1, \mathbf{k}_2, \hat{s}) \Phi(\mathbf{k}_{J2}, x_{J2}, \mathbf{k}_2)$$

- $n = 0 \implies$ differential cross-section

$$C_0 = \frac{d\sigma}{d|\mathbf{k}_{J1}| d|\mathbf{k}_{J2}| dy_{J1} dy_{J2}}$$

- $n > 0 \implies$ azimuthal decorrelation

$$\frac{C_n}{C_0} = \langle \cos(n(\phi_{J,1} - \phi_{J,2} - \pi)) \rangle \equiv \langle \cos(n\varphi) \rangle$$

- sum over $n \implies$ azimuthal distribution

$$\frac{1}{\sigma} \frac{d\sigma}{d\varphi} = \frac{1}{2\pi} \left\{ 1 + 2 \sum_{n=1}^{\infty} \cos(n\varphi) \langle \cos(n\varphi) \rangle \right\}$$