

# Hard exclusive processes

Samuel Wallon

Université Pierre et Marie Curie  
and  
Laboratoire de Physique Théorique  
CNRS / Université Paris Sud  
Orsay

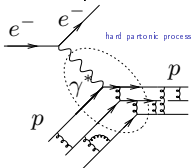
International Symposium on Multiparticle Dynamics

Kielce, September 20th 2012

# Exclusive processes are challenging

Can one extract information on hadrons using **hard** exclusive processes?

- The aim is to reduce the process to interactions involving a small number of *partons* (quarks, gluons), despite confinement
- This is possible if the considered process is driven by short distance phenomena ( $d \ll 1 \text{ fm}$ )  
 $\implies \alpha_s \ll 1$  : **Perturbative methods**
- One should hit strongly enough a hadron  
 Example: electromagnetic probe and form factor



$\tau$  electromagnetic interaction  $\sim \tau$  parton life time after interaction  
 $\ll \tau$  characteristic time of strong interaction

To get such situations in exclusive reactions is very challenging:  
 the cross section are very small

## Counting rules

## The partonic point of view... and its limitations

- Counting rules:

$$F_n(q^2) \simeq \frac{C}{(Q^2)^{n-1}} \quad n = \text{number of minimal constituents: } \begin{cases} \text{meson: } n = 2 \\ \text{baryon: } n = 3 \end{cases}$$

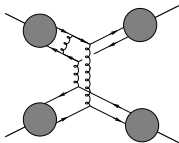
Brodsky, Farrar '73

- Large angle** (i.e.  $s \sim t \sim u$  large) elastic processes  $h_a h_b \rightarrow h_a h_b$   
e.g. :  $\pi\pi \rightarrow \pi\pi$  or  $pp \rightarrow pp$

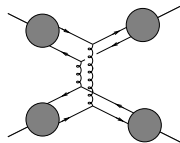
$$\frac{d\sigma}{dt} \sim \left( \frac{\alpha_S(p_\perp^2)}{s} \right)^{n-2} \quad n = \# \text{ of external fermionic lines } (n = 8 \text{ for } \pi\pi \rightarrow \pi\pi)$$

Brodsky, Lepage '81

Other contributions might be significant, even at large angle: e.g.  $\pi\pi \rightarrow \pi\pi$



Brodsky Lepage mechanism:  $\frac{d\sigma_{BL}}{dt} \sim \left( \frac{1}{s} \right)^6$



Lanshoff '74 mechanism:  $\frac{d\sigma_L}{dt} \sim \left( \frac{1}{s} \right)^5$

absent with at least one  $\gamma^{(*)}$  (point-like coupling)

# From inclusive to exclusive processes

## Experimental effort

- Inclusive processes are not  $1/Q$  suppressed (e.g. DIS)
- Going from inclusive to exclusive processes is **difficult**
- **High luminosity accelerators and high-performance detection facilities**  
HERA (H1, ZEUS), HERMES, JLab@6 GeV (Hall A, CLAS), BaBar, Belle, BEPC-II (BES-III)  
future: LHC, COMPASS-II, JLab@12 GeV, Super-B, LHeC, EIC, ILC
- What to do, and where?
  - Proton form factor: JLab@6 GeV future: PANDA (timelike proton form factor through  $p\bar{p} \rightarrow e^+e^-$ )
  - $e^+e^-$  in  $\gamma^*\gamma$  single-tagged channel: Transition form factor  $\gamma^*\gamma \rightarrow \pi$ , exotic hybrid meson production BaBar, Belle, BES,...
  - Deep Virtual Compton Scattering (GPD)  
HERA (H1, ZEUS), HERMES, JLab@6 GeV  
future: JLab@12GeV, COMPASS-II, EIC
  - Non exotic and exotic hybrid meson electroproduction (GPD and DA), etc...  
NMC (CERN), E665 (Fermilab), HERA (H1, ZEUS), COMPASS, HERMES, CLAS (JLab)
  - TDA (PANDA at GSI)
  - TMDs (BaBar, Belle, COMPASS, ...)
  - Diffractive processes, including ultraperipheral collisions  
LHC (with or without fixed targets), ILC

# From inclusive to exclusive processes

## Theoretical efforts

Very important theoretical developments during the last decade

- Key words:

DAs, GPDs, GDAs, TDAs ... TMDs

- Fundamental tools:

- At medium energies (for a particle physicist!):

JLab, HERMES, COMPASS, BaBar, Belle, PANDA, Super-B, EIC

collinear factorization

- At asymptotical energies:

HERA, Tevatron, LHC, LHeC, ILC (EIC and COMPASS at the boundary)

$k_T$ -factorization

## Extensions from DIS

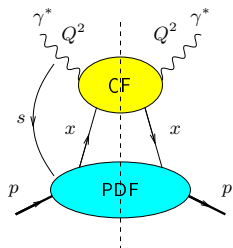
- DIS: inclusive process  $\rightarrow$  forward amplitude ( $t = 0$ ) (optical theorem)

(DIS: Deep Inelastic Scattering)

ex:  $e^\pm p \rightarrow e^\pm X$  at HERA

Structure Function

$$= \text{Coefficient Function (hard)} \otimes \text{Parton Distribution Function (soft)}$$

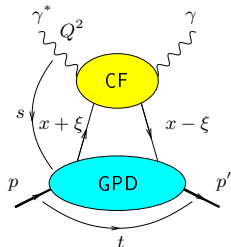


- DVCS: exclusive process  $\rightarrow$  non forward amplitude ( $-t \ll s = W^2$ )

(DVCS: Deep Virtual Compton Scattering)

Amplitude

$$= \text{Coefficient Function (hard)} \otimes \text{Generalized Parton Distribution (soft)}$$



Müller et al. '91 - '94; Radyushkin '96; Ji '97

## Extensions from DVCS

- **Meson production:**  $\gamma$  replaced by  $\rho, \pi, \dots$

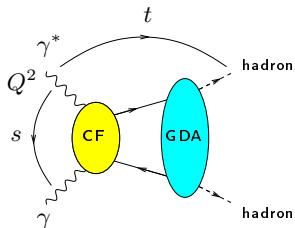
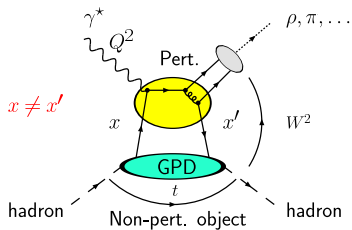
$$\text{Amplitude} = \text{GPD (soft)} \otimes \text{CF (hard)} \otimes \text{Distribution Amplitude (soft)}$$

Collins, Frankfurt, Strikman '97; Radyushkin '97

- **Crossed process:**  $s \ll -t$

$$\text{Amplitude} = \text{Coefficient Function (hard)} \otimes \text{Generalized Distribution Amplitude (soft)}$$

Diehl, Gousset, Pire, Teryaev '98



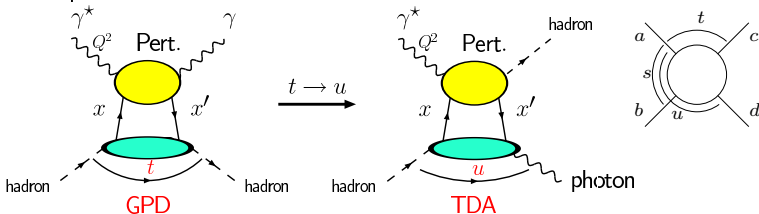
## Extensions from DVCS

- Starting from usual DVCS, one allows: initial hadron  $\neq$  final hadron (in the same octuplet): transition GPDs

Even less diagonal:

baryonic number (initial state)  $\neq$  baryonic number (final state)  $\rightarrow$  TDA

Example:



Pire, Szymanowski '05

which can be further extended by replacing the outgoing  $\gamma$  by any hadronic state

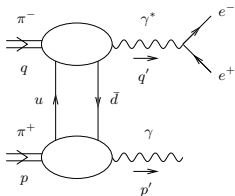
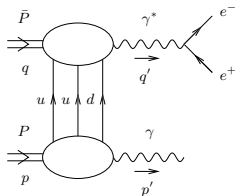
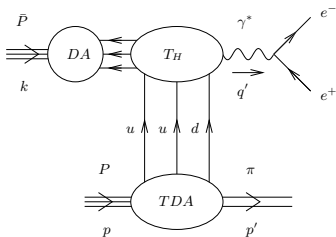
$$\text{Amplitude} = \text{Transition Distribution Amplitude (soft)} \otimes \text{CF (hard)} \otimes \text{DA (soft)}$$

Lansberg, Pire, Szymanowski '06



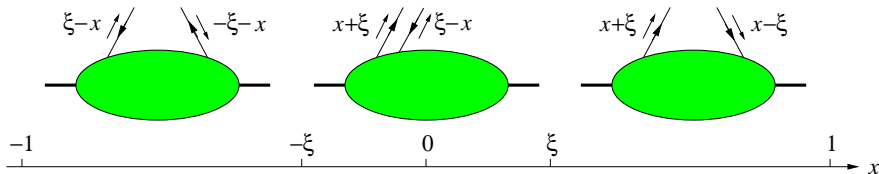
## Extensions from DVCS

## TDA at PANDA

TDA  $\pi \rightarrow \gamma$ TDA  $p \rightarrow \gamma$  at PANDA (forward scattering of  $\bar{p}$  on a  $p$  probe)TDA  $p \rightarrow \pi$  at PANDA (forward scattering of  $\bar{p}$  on a  $p$  probe)Spectral model for the  $p \rightarrow \pi$  TDA: Pire, Semenov, Szymanowski '10

## Twist 2 GPDs

## Physical interpretation for GPDs



Emission and reabsorption  
of an antiquark  
~ PDFs for antiquarks  
DGLAP-II region

Emission of a quark and  
emission of an antiquark  
~ meson exchange  
ERBL region

Emission and reabsorption  
of a quark  
~ PDFs for quarks  
DGLAP-I region

## Twist 2 GPDs

## Classification of twist 2 GPDs

- For quarks, one should distinguish the exchanges
  - without helicity flip (chiral-even  $\Gamma'$  matrices): 4 chiral-even GPDs:

$H^q \xrightarrow{\xi=0, t=0}$  PDF  $q$ ,  $E^q$ ,  $\tilde{H}^q \xrightarrow{\xi=0, t=0}$  polarized PDFs  $\Delta q$ ,  $\tilde{E}^q$

$$\begin{aligned} F^q &= \frac{1}{2} \int \frac{dz^+}{2\pi} e^{ixP^- z^+} \langle p' | \bar{q}(-\frac{1}{2}z) \gamma^- q(\frac{1}{2}z) | p \rangle \Big|_{z^-=0, z_\perp=0} \\ &= \frac{1}{2P^-} \left[ H^q(x, \xi, t) \bar{u}(p') \gamma^- u(p) + E^q(x, \xi, t) \bar{u}(p') \frac{i \sigma^{-\alpha} \Delta_\alpha}{2m} u(p) \right], \end{aligned}$$

$$\begin{aligned} \tilde{F}^q &= \frac{1}{2} \int \frac{dz^+}{2\pi} e^{ixP^- z^+} \langle p' | \bar{q}(-\frac{1}{2}z) \gamma^- \gamma_5 q(\frac{1}{2}z) | p \rangle \Big|_{z^-=0, z_\perp=0} \\ &= \frac{1}{2P^-} \left[ \tilde{H}^q(x, \xi, t) \bar{u}(p') \gamma^- \gamma_5 u(p) + \tilde{E}^q(x, \xi, t) \bar{u}(p') \frac{\gamma_5 \Delta^-}{2m} u(p) \right]. \end{aligned}$$

- with helicity flip (chiral-odd  $\Gamma'$  mat.): 4 chiral-odd GPDs:

$H_T^q \xrightarrow{\xi=0, t=0}$  quark transversity PDFs  $\Delta_T q$ ,  $E_T^q$ ,  $\tilde{H}_T^q$ ,  $\tilde{E}_T^q$

$$\begin{aligned} &\frac{1}{2} \int \frac{dz^+}{2\pi} e^{ixP^- z^+} \langle p' | \bar{q}(-\frac{1}{2}z) i \sigma^{-i} q(\frac{1}{2}z) | p \rangle \Big|_{z^-=0, z_\perp=0} \\ &= \frac{1}{2P^-} \bar{u}(p') \left[ H_T^q i \sigma^{-i} + \tilde{H}_T^q \frac{P^- \Delta^i - \Delta^- P^i}{m^2} + E_T^q \frac{\gamma^- \Delta^i - \Delta^- \gamma^i}{2m} + \tilde{E}_T^q \frac{\gamma^- P^i - P^- \gamma^i}{m} \right] \end{aligned}$$

## Twist 2 GPDs

## Classification of twist 2 GPDs

- analogously, for gluons:

- 4 gluonic GPDs without helicity flip:

$$H^g \xrightarrow{\xi=0, t=0} \text{PDF } x g$$

$$E^g$$

$$\tilde{H}^g \xrightarrow{\xi=0, t=0} \text{polarized PDF } x \Delta g$$

$$\tilde{E}^g$$

- 4 gluonic GPDs with helicity flip:

$$H_T^g$$

$$E_T^g$$

$$\tilde{H}_T^g$$

$$\tilde{E}_T^g$$

(no forward limit reducing to gluons PDFs here: a change of 2 units of helicity cannot be compensated by a spin 1/2 target)

## Spin transversity in the nucleon

## What is transversity?

- Transverse spin content of the proton:

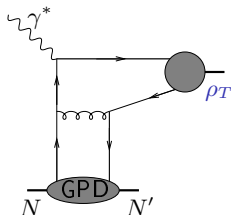
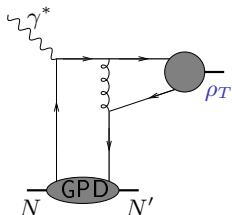
$$\begin{array}{lcl} |\uparrow\rangle_{(x)} & \sim & |\rightarrow\rangle + |\leftarrow\rangle \\ |\downarrow\rangle_{(x)} & \sim & |\rightarrow\rangle - |\leftarrow\rangle \\ \text{spin along } x & & \text{helicity state} \end{array}$$

- An observable sensitive to helicity spin flip gives thus access to the transversity  $\Delta_T q(x)$ , which is very badly known (first data have recently been obtained by COMPASS)
- The transversity GPDs are completely unknown
- **Chirality:**  $q_{\pm}(z) \equiv \frac{1}{2}(1 \pm \gamma^5)q(z)$  with  $q(z) = q_+(z) + q_-(z)$   
Chiral-even: **chirality conserving**  
 $\bar{q}_{\pm}(z)\gamma^{\mu}q_{\pm}(-z)$  and  $\bar{q}_{\pm}(z)\gamma^{\mu}\gamma^5q_{\pm}(-z)$   
Chiral-odd: **chirality reversing**  
 $\bar{q}_{\pm}(z) \cdot 1 \cdot q_{\mp}(-z)$ ,  $\bar{q}_{\pm}(z) \cdot \gamma^5 \cdot q_{\mp}(-z)$  and  $\bar{q}_{\pm}(z)[\gamma^{\mu}, \gamma^{\nu}]q_{\mp}(-z)$
- For a massless (anti)particle, chirality = (-)helicity
- **Transversity is thus a chiral-odd quantity**
- QCD and QED are chiral even  $\Rightarrow \mathcal{A} \sim (\text{Ch.-odd})_1 \otimes (\text{Ch.-odd})_2$

# Accessing transversity in the nucleon

## How to get access to transversity?

- The dominant DA for  $\rho_T$  is of twist 2 and chiral-odd ( $[\gamma^\mu, \gamma^\nu]$  coupling)
- Unfortunately  $\gamma^* N^\dagger \rightarrow \rho_T N' = 0$ 
  - this is true at any order in perturbation theory (i.e. corrections as powers of  $\alpha_s$ ), since this would require a transfer of 2 units of helicity from the proton: impossible! Collins, Diehl '00
  - diagrammatic argument at Born order:



vanishes:  $\gamma^\alpha [\gamma^\mu, \gamma^\nu] \gamma_\alpha = 0$

Diehl, Gousset, Pire '99

# Accessing transversity in the nucleon

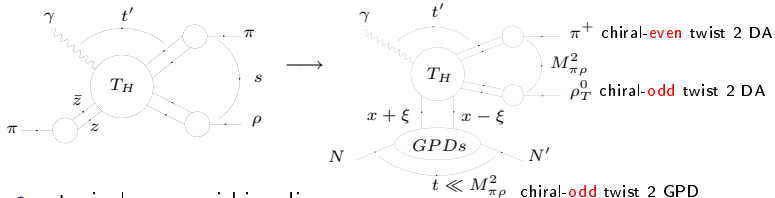
## Can one circumvent this vanishing?

- This vanishing is true only a twist 2
- At twist 3 this process does not vanish
- However processes involving twist 3 DAs may face problems with factorization (end-point singularities: see later)
- The problem of classification of twist 3 chiral-odd GPDs is still open:  
Pire, Szymanowski, S.W. in progress, in the spirit of our framework recently developed:  
**Light-Cone Collinear Factorization**  
Anikin, Ivanov, Pire, Szymanowski, S. W.  
Phys. Lett. B682:413-418, 2010; Nucl.Phys. B 828:1-68, 2010

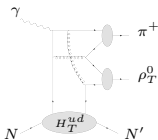
# Accessing transversity in the nucleon

$\gamma N \rightarrow \pi^+ \rho_T^0 N'$  gives access to transversity

- Factorization à la **Brodsky Lepage** of  $\gamma + \pi \rightarrow \pi + \rho$  at large  $s$  and fixed angle (i.e. fixed ratio  $t'/s, u'/s$ )  
 $\implies$  factorization of the amplitude for  $\gamma + N \rightarrow \pi + \rho + N'$  at large  $M_{\pi\rho}^2$



- a typical non-vanishing diagram:



M. El Beiyad, P. Pire, M. Segond, L. Szymanowski, S.W. Phys.Lett.B688:154-167,2010

see also, at large  $s$ , with Pomeron exchange:

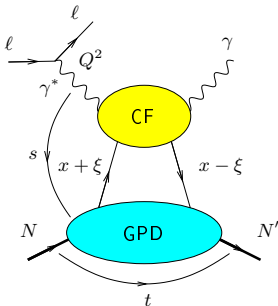
R. Ivanov, B. Pire, L. Symanowski, O. Teryaev '02

R. Enberg, B. Pire, L. Symanowski '06

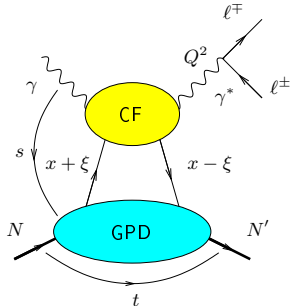
- These processes with 3 body final state can give access to all GPDs:  $M_{\pi\rho}^2$  plays the role of the  $\gamma^*$  virtuality of usual DVCS (here in the time-like domain) JLab, COMPASS



## DVCS and TCS



Deeply Virtual Compton Scattering  
 $lN \rightarrow l'N'\gamma$

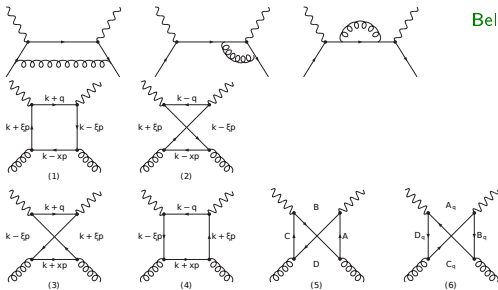


Timelike Compton Scattering  
 $\gamma N \rightarrow l^+l^-N'$

- TCS versus DVCS:
  - universality of the GPDs
  - another source for GPDs (special sensitivity on real part)
  - spacelike-timelike crossing and understanding the structure of the NLO corrections
- Where to measure TCS? In Ultra Peripheral Collisions  
LHC, JLab, COMPASS, AFTER

## DVCS and TCS at NLO

## One loop contributions



Belitsky, Mueller, Niedermeier, Schafer,  
Phys.Lett.B474, 2000  
Pire, Szymanowski, Wagner  
Phys.Rev.D83, 2011

$$\mathcal{A}^{\mu\nu} = g_T^{\mu\nu} \int_{-1}^1 dx \left[ \sum_q^{n_F} T^q(x) F^q(x) + T^g(x) F^g(x) \right]$$

## Resummations effects are expected

- The renormalized quark **coefficient functions**  $T^q$  is

$$T^q = C_0^q + C_1^q + C_{coll}^q \log \frac{|Q^2|}{\mu_F^2}$$

$$C_0^q = e_q^2 \left( \frac{1}{x - \xi + i\epsilon} - (x \rightarrow -x) \right)$$

$$C_1^q = \frac{e_q^2 \alpha_S C_F}{4\pi(x - \xi + i\epsilon)} \left[ \log^2 \left( \frac{\xi - x}{2\xi} - i\epsilon \right) + \dots \right] - (x \rightarrow -x)$$

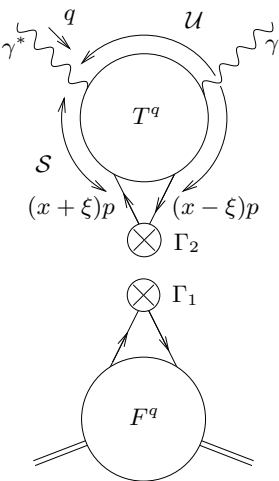
- Usual collinear approach: single-scale analysis w.r.t.  $Q^2$
- Consider the invariants  $S$  and  $U$ :

$$S = \frac{x - \xi}{2\xi} Q^2 \ll Q^2 \quad \text{when } x \rightarrow \xi$$

$$U = -\frac{x + \xi}{2\xi} Q^2 \ll Q^2 \quad \text{when } x \rightarrow -\xi$$

⇒ **two scales problem; threshold singularities to be resummed**

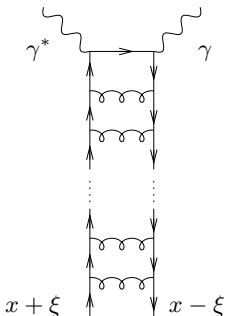
analogous to the  $\log(x - x_{Bj})$  resummation for DIS coefficient functions



## Resummation for Coefficient functions

## Soft-collinear resummation effects for the coefficient function

- The resummation easier when using the axial gauge  $p_1 \cdot A = 0$  ( $p_\gamma \equiv p_1$ )
- The dominant diagram are ladder-like



resummed formula (for DVCS), for  $x \rightarrow \xi$  :

$$\begin{aligned}
 (T^q)^{\text{res}} = & \left( \frac{e_q^2}{x - \xi + i\epsilon} \left\{ \cosh \left[ D \log \left( \frac{\xi - x}{2\xi} - i\epsilon \right) \right] \right. \right. \\
 & \left. \left. - \frac{D^2}{2} \left[ 9 + 3 \frac{\xi - x}{x + \xi} \log \left( \frac{\xi - x}{2\xi} - i\epsilon \right) \right] \right\} \right. \\
 & \left. + C_{\text{coll}}^q \log \frac{Q^2}{\mu_F^2} \right) - (x \rightarrow -x) \quad \text{with} \quad D = \sqrt{\frac{\alpha_s C_F}{2\pi}}
 \end{aligned}$$

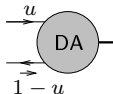
T. Altinoluk, B. Pire, L. Szymanowski, S. W.  
to appear in JHEP [arXiv:1207.4609]; [arXiv:1206.3115]

- Moment space (Gegenbauer polynomials) ??  
unknown analog of the  $N$ -Mellin space for  $x_{Bj} \rightarrow 1$  in DIS

## $\rho$ -electroproduction: Selection rules and factorization status

- chirality = helicity for a particle, chirality =  $\ominus$  helicity for an **antiparticle**
- for massless quarks: **QED and QCD vertices = chiral even** (no chirality flip during the interaction)
  - $\Rightarrow$  the total helicity of a  $q\bar{q}$  produced by a  $\gamma^*$  should be 0
  - $\Rightarrow$  helicity of the  $\gamma^* = L_z^{q\bar{q}}$  ( $z$  projection of the  $q\bar{q}$  angular momentum)
- in the pure collinear limit (i.e. twist 2),  $L_z^{q\bar{q}}=0 \Rightarrow \gamma_L^*$
- at  $t = 0$ , no source of orbital momentum from the proton coupling  $\Rightarrow$  **helicity of the meson = helicity of the photon**
- in the collinear factorization approach,  $t \neq 0$  change nothing from the hard side  $\Rightarrow$  the above selection rule remains true
- thus: 2 transitions possible ( $s$ -channel helicity conservation (SCHC)):
  - $\gamma_L^* \rightarrow \rho_L$  transition: QCD factorization **holds at  $t=2$**  at any order in perturbation (i.e. LL, NLL, etc...)
  - Collins, Frankfurt, Strikman '97 Radyushkin '97**
  - $\gamma_T^* \rightarrow \rho_T$  transition: QCD factorization **has problems at  $t=3$**
  - Mankiewicz-Piller '00**

$$\int_0^1 \frac{du}{u} \text{ or } \int_0^1 \frac{du}{1-u} \text{ diverge (end-point singularity)}$$



# $\rho$ -electroproduction: Selection rules and factorization status

## Improved collinear approximation: a solution?

- keep a transverse  $\ell_{\perp}$  dependency in the  $q, \bar{q}$  momenta, used to regulate end-point singularities
- soft and collinear gluon exchange between the valence quark are responsible for large double-logarithmic effects which are conjectured to exponentiate
- this is made easier when using the impact parameter space  $b_{\perp}$  conjugated to  $\ell_{\perp} \Rightarrow$  Sudakov factor

$$\exp[-S(u, b, Q)]$$

- $S$  diverges when  $b_{\perp} \sim O(1/\Lambda_{QCD})$  (large transverse separation, i.e. small transverse momenta) or  $u \sim O(\Lambda_{QCD}/Q)$  Botts, Sterman '89  
 $\Rightarrow$  regularization of end-point singularities for  $\pi \rightarrow \pi\gamma^*$  and  $\gamma\gamma^*\pi^0$  form factors, based on the factorization approach Li, Sterman '92
- it has been proposed to combine this perturbative resummation tail effect with an ad-hoc non-perturbative gaussian ansatz for the DAs

$$\exp[-a^2 |k_{\perp}^2|/(u\bar{u})]$$

which gives back the usual asymptotic DA  $6u\bar{u}$  when integrating over  $k_{\perp}$   
 $\Rightarrow$  practical tools for meson electroproduction phenomenology

Goloskokov, Kroll '05

## Theoretical motivations

A particular regime for QCD:  
The perturbative Regge limit  $s \rightarrow \infty$

Consider the diffusion of two hadrons  $h_1$  and  $h_2$ :

- $\sqrt{s}$  ( $= E_1 + E_2$  in the center-of-mass system)  $\gg$  other scales (masses, transferred momenta, ...) eg  $x_B \rightarrow 0$  in DIS
- other scales comparable (virtualities, etc...)  $\gg \Lambda_{QCD}$

regime  $\alpha_s \ln s \sim 1 \Rightarrow$  dominant sub-series:

$$\mathcal{A} = \underbrace{\text{Diagram 1}}_{\sim s} + \left( \underbrace{\text{Diagram 2}}_{\sim s} + \underbrace{\text{Diagram 3}}_{\sim s} + \dots \right) + \left( \underbrace{\text{Diagram 4}}_{\sim s} + \dots \right) + \dots$$

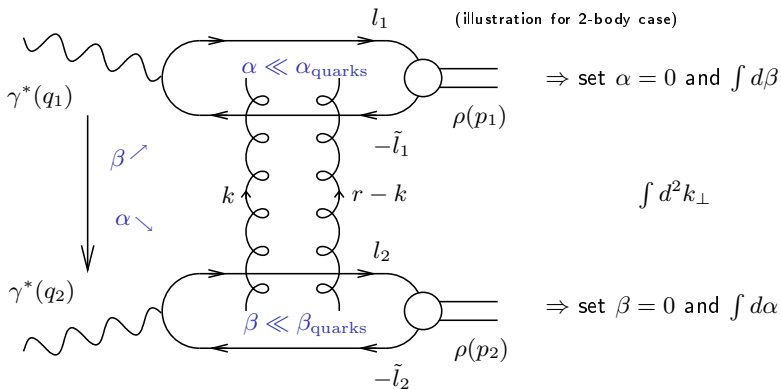
$\Rightarrow \sigma_{tot}^{h_1 h_2 \rightarrow tout} = \frac{1}{s} \text{Im} \mathcal{A} \sim s^{\alpha_P(0)-1}$

with  $\alpha_P(0) - 1 = C \alpha_s$  ( $C > 0$ ) hard Pomeron (Balitsky, Fadin, Kuraev, Lipatov '75)

- This result violates QCD  $S$  matrix unitarity ( $S S^\dagger = S^\dagger S = 1$  i.e.  $\sum \text{Prob.} = 1$ )
- Until when this result could be applicable, and how to improve it?
- How to test this dynamics experimentally, in particular based on exclusive processes?

$k_T$  factorization $\gamma^* \gamma^* \rightarrow \rho\rho$  as an example

- Use **Sudakov** decomposition  $k = \alpha p_1 + \beta p_2 + k_\perp$  ( $p_1^2 = p_2^2 = 0$ ,  $2p_1 \cdot p_2 = s$ )
- write 
$$d^4k = \frac{s}{2} d\alpha d\beta d^2k_\perp$$
- $t$ -channel gluons with **non-sense** polarizations ( $\epsilon_{NS}^{up} = \frac{2}{s} p_2$ ,  $\epsilon_{NS}^{down} = \frac{2}{s} p_1$ ) dominate **at large  $s$**



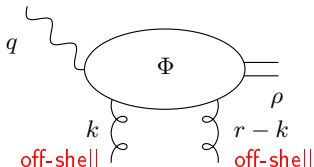


$k_T$  factorization

Impact representation for exclusive processes  $\underline{k} = \text{Eucl.} \leftrightarrow k_{\perp} = \text{Mink.}$

$$\mathcal{M} = is \int \frac{d^2 \underline{k}}{(2\pi)^2 \underline{k}^2 (\underline{r} - \underline{k})^2} \Phi^{\gamma^*(q_1) \rightarrow \rho(p_1^{\rho})}(\underline{k}, \underline{r} - \underline{k}) \Phi^{\gamma^*(q_2) \rightarrow \rho(p_2^{\rho})}(-\underline{k}, -\underline{r} + \underline{k})$$

$\Phi^{\gamma^*(q_1) \rightarrow \rho(p_1^{\rho})}$ :  $\gamma_{L,T}^*(q)g(k_1) \rightarrow \rho_{L,T}g(k_2)$  impact factor



## Meson production at HERA

## Diffractive meson production at HERA

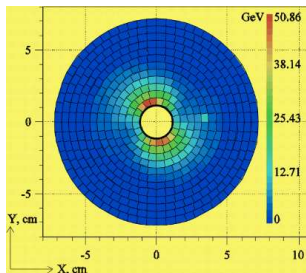
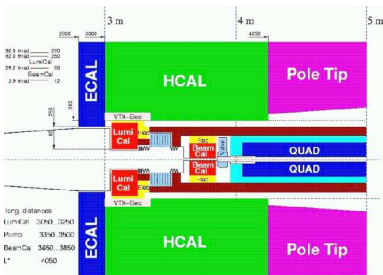
HERA (DESY, Hamburg): first and single  $e^\pm p$  collider (1992-2007)

- The "easy" case (from factorization point of view):  $J/\Psi$  production ( $u \sim 1/2$ : non-relativistic limit for bound state) combined with  $k_T$ -factorisation  
Ryskin '93; Frankfurt, Koepf, Strikman '98; Ivanov, Kirschner, Schäfer, Szymanowski '00; Motyka, Enberg, Poludniowski '02
- Exclusive vector meson photoproduction at large  $t$  (= hard scale):  
 $\gamma(q) + P \rightarrow \rho_{L,T}(p_1) + P$   
based on  $k_T$ -factorization:  
Forshaw, Ryskin '95; Bartels, Forshaw, Lotter, Wüsthoff '96; Forshaw, Motyka, Enberg, Poludniowski '03
  - H1, ZEUS data seems to favor BFKL
  - but end-point singularities for  $\rho_T$  are regularized with a quark mass:  
 $m = m_\rho/2$
  - the spin density matrix is badly described
- Exclusive electroproduction of vector meson  
 $\gamma_{L,T}^*(q) + P \rightarrow \rho_{L,T}(p_1) + P$  Goloskokov, Kroll '05  
based on improved collinear factorization for the coupling with the meson DA and collinear factorization for GPD coupling

Phenomenological applications: exclusive test of  $\mathbb{P}$ omeron

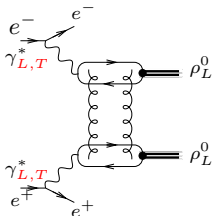
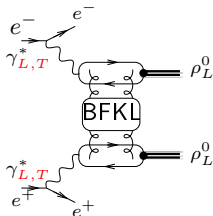
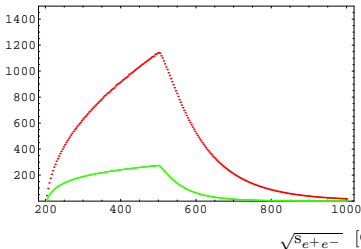
An example of realistic exclusive test of  $\mathbb{P}$ omeron:  $\gamma^{(*)}\gamma^{(*)} \rightarrow \rho\rho$   
as a subprocess of  $e^-e^+ \rightarrow e^-e^+ \rho_L^0 \rho_L^0$

- ILC should provide  $\left\{ \begin{array}{l} \text{very large } \sqrt{s} (= 500 \text{ GeV}) \\ \text{very large luminosity } (\simeq 125 \text{ fb}^{-1}/\text{year}) \end{array} \right.$
- detectors are planned to cover the **very forward** region, close from the beampipe (directions of out-going  $e^+$  and  $e^-$  at large  $s$ )



good efficiency of tagging for outgoing  $e^\pm$  for  $E_e > 100 \text{ GeV}$  and  $\theta > 4 \text{ mrad}$   
(illustration for LDC concept)

- could be equivalently done at LHC based on the AFP project

Phenomenological applications: exclusive test of  $\mathbb{P}$  PomeronQCD effects in the Regge limit on  $\gamma^{(*)}\gamma^{(*)} \rightarrow \rho\rho$  $\simeq 4 \cdot 10^3$  events/year $\simeq 2 \cdot 10^4$  events/year $\frac{d\sigma^{tmin}}{dt} (fb/GeV^2)$ 

proof of feasibility:

B. Pire, L. Szymanowski and S. W.  
Eur.Phys.J.C44 (2005) 545

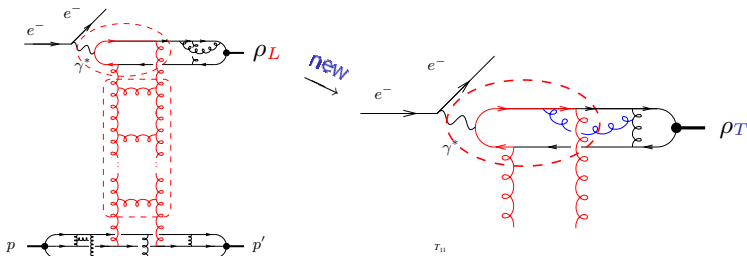
proof of visible BFKL enhancement:

R. Enberg, B. Pire, L. Szymanowski and S. W.  
Eur.Phys.J.C45 (2006) 759comprehensive study of  $\gamma^*$  polarization effects  
and event rates:M. Segond, L. Szymanowski and S. W.  
Eur. Phys. J. C 52 (2007) 93

NLO BFKL study:

Ivanov, Papa '06 '07; Caporale, Papa, Vera '08

## Exclusive vector meson production at HERA

Diffractive exclusive process  $e^- p \rightarrow e^- p \rho_{L,T}$ 

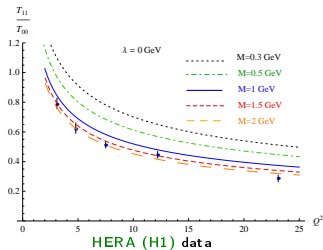
first description combining beyond leading twist

- collinear factorisation
- $k_T$ -factorisation

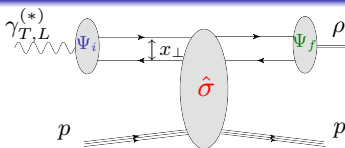
I. V. Anikin, D. Yu. Ivanov, B. Pire, L. Szymanowski, S.W.

Phys.Lett.B682 (2010) 413-418  
Nucl.Phys.B828 (2010) 1-68

HERA, LHeC, AFP@LHC

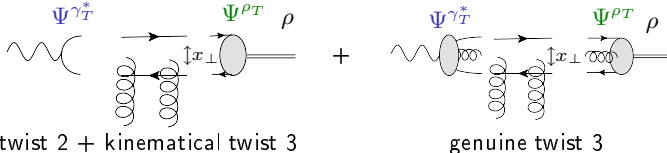
I. V. Anikin, A. Besse, D. Yu. Ivanov, B. Pire,  
L. Szymanowski, S.W.  
Phys.Rev. D84 (2011) 054004

## Dipole representation and saturation effects



Nikolaev, Zakharov '91

- Initial  $\Psi_i$  and final  $\Psi_f$  states wave functions of projectiles
- Universal scattering amplitude  $\hat{\sigma} \equiv \hat{\sigma}_{\text{dipole-target}}$  Golec-Biernat Wusthoff
  - color transparency for small  $x_{\perp}$ :  $\hat{\sigma}_{\text{dipole-target}} \sim x_{\perp}^2$
  - saturation for large  $x_{\perp} \sim 1/Q_{\text{sat}}$ :  $T < 1$
- Data for  $\rho$  prod. calls for models encoding saturation  
Munier, Stasto, Mueller '04; Kowalski, Motyka, Watt '06
- The dipole repr. is consistent with the twist 2 collinear factorization
- **New: still consistent with collinear factorization at higher twist order:**



twist 2 + kinematical twist 3

genuine twist 3

A. Besse, L. Szymanowski, S. W., arXiv:1204.2281 [hep-ph], to appear in NPB

Phenomenology: A. Besse, L. Szymanowski, S. W. in preparation

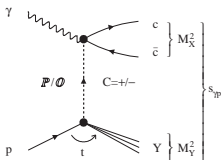
 $\gamma$  case for large  $|t|$ ?  $b$ -dependence?

# Finding the hard Odderon

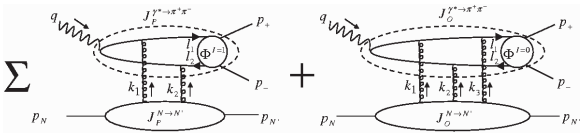
- colorless gluonic exchange
  - $C = +1$  : Pomeron, in pQCD described by **BFKL** equation
  - $C = -1$  : Odderon, in pQCD described by **BJKP** equation
- best but still weak evidence for  $\mathbb{O}$ :  $pp$  and  $p\bar{p}$  data at **ISR**
- no evidence for perturbative  $\mathbb{O}$

# Finding the hard Odderon

- exchange much weaker than  $\mathbb{P} \Rightarrow$  two strategies in QCD
  - consider **processes**, where  $\mathbb{P}$  vanishes due to  $C$ -parity conservation:
    - exclusive  $\eta, \eta_c, f_2, a_2, \dots$  in  $ep$ ;  $\gamma\gamma \rightarrow \eta_c \eta_c \sim |\mathcal{M}_\mathbb{O}|^2$  Braunewell, Ewerz '04
    - exclusive  $J/\Psi, \Upsilon$  in  $pp$  ( $\mathbb{P}\mathbb{O}$  fusion, not  $\mathbb{P}\mathbb{P}$ ) Bzdak, Motyka, Szymanowski, Cudell '07
  - consider **observables** sensitive to the **interference** between  $\mathbb{P}$  and  $\mathbb{O}$  (open charm in  $ep$ ;  $\pi^+\pi^-$  in  $ep$ )  $\sim \text{Re} \mathcal{M}_\mathbb{P} \mathcal{M}_\mathbb{O}^* \Rightarrow$  observable **linear** in  $\mathcal{M}_\mathbb{O}$



Brodsky, Rathsman, Merino '99



Ivanov, Nikolaev, Ginzburg '01 in photo-production

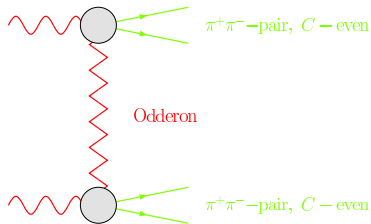
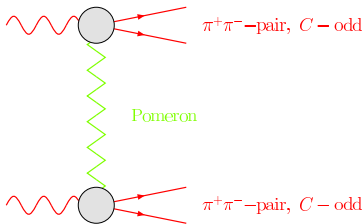
Hägler, Pire, Szymanowski, Teryaev '02 in electro-production



# Finding the hard Odderon

## $\mathbb{P} - \mathbb{O}$ interference in double UPC

$\mathbb{P} - \mathbb{O}$  interference in  $\gamma\gamma \rightarrow \pi^+ \pi^- \pi^+ \pi^-$



Hard scale =  $t$

B. Pire, F. Schwennsen, L. Szymanowski, S. W.

Phys.Rev.D78:094009 (2008)

pb at LHC: pile-up!

# Conclusion

- Since a decade, there have been much progress in the understanding of **hard** exclusive processes
  - at medium energies, there is now a conceptual framework starting from first principle, allowing to describe a huge number of processes
  - at high energy, the impact representation is a powerful tool for describing exclusive processes in diffractive experiments; they are and will be essential for studying QCD in the hard Regge limit (Pomeron, Odderon, saturation...)
- till, some problems remain:
  - proofs of factorization have been obtained only for very few processes (ex.:  $\gamma^* p \rightarrow \gamma p$ ,  $\gamma_L^* p \rightarrow \rho_L p$ )
  - for some other processes factorization is highly plausible, but not fully demonstrated at any order (ex.: processes involving GDAs and TDAs)
  - some processes explicitly show sign of breaking of factorization (ex.:  $\gamma_T^* p \rightarrow \rho_T p$  which has end-point singularities at Leading Order)
  - models and results from the lattice for the non-perturbative correlators entering GPDs, DAs, GDAs, TDAs are needed, even at a qualitative level!
  - the effect of QCD evolution, the NLO corrections with potential resummation effects, choice of renormalization/factorization scale, power corrections will be very relevant to interpret and describe the forthcoming data
- Links between theoretical and experimental communities are very fruitful  
HERA, HERMES, Tevatron, LHC, JLab, COMPASS, BaBar, BELLE, Super-B, EIC, LHeC, ILC  
This is very hot and pleasant domain. Everybody is welcome!